

# Atmospheric Aerosols I

*Required reading: Jacob Chapter 8*

Atmospheric chemistry  
ATOC-5151 / CHEM-5151  
Spring 2013  
Prof. J.L. Jimenez

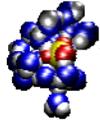
Some slides adapted from lectures from Qi Zhang, Daniel Jacob, and Sergey Nidkorodov

## Business Items

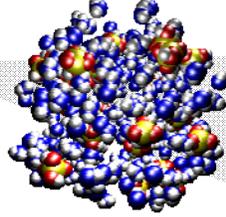
- HW#6 will be assigned later today
  - Due in 2 weeks
  - 2 problems + 1 bonus problem
- Final will be cumulative
- HW4 and 5 to be sent back soon
- Midterm not graded yet, hopefully this week
- Other questions?

## From molecules to particles: nucleation

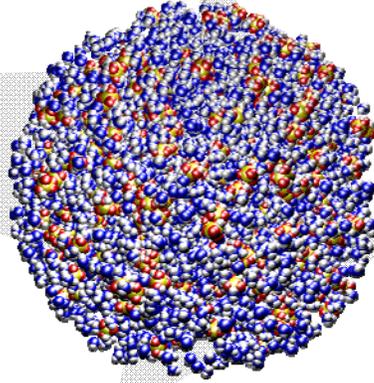
$\text{H}_2\text{SO}_4 (\text{H}_2\text{O})_{20}$   
a typical  
critical cluster



$(\text{H}_2\text{SO}_4)_{25} (\text{H}_2\text{O})_{250}$   
a nucleated  
particle that is  
growing



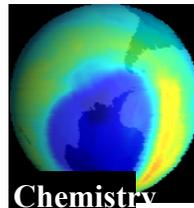
$4\text{nm} + 6\text{ nm}$   
 $(\text{H}_2\text{SO}_4)_{500} (\text{H}_2\text{O})_{4000}$   
a nanodroplet of aqueous  
sulfuric acid



- Nucleation creates new atmospheric aerosol
- Fundamental understanding of nucleation is limited
- Binary nucleation of  $\text{H}_2\text{SO}_4$  and  $\text{H}_2\text{O}$  is important in free troposphere

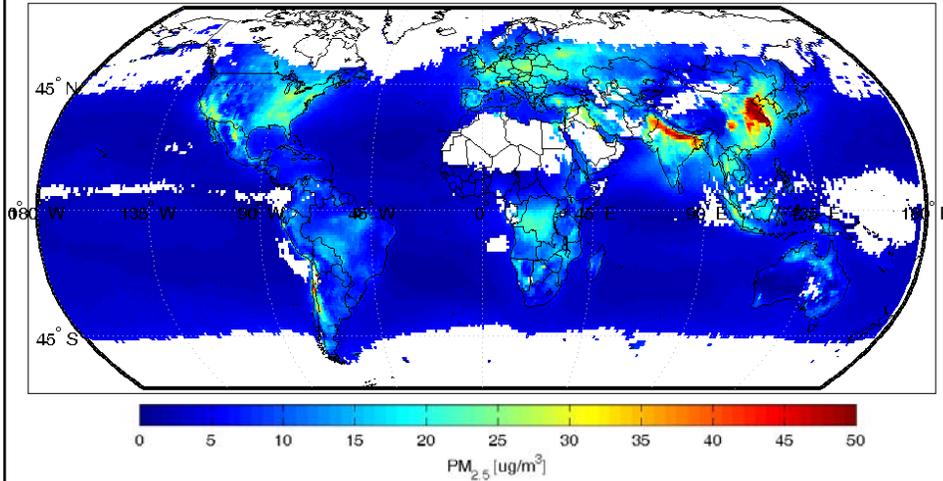
Slide courtesy of Shawn  
Katzman (PNNL)

## Why care about atmospheric aerosols?



From Jacob

ANNUAL MEAN PM<sub>2.5</sub> CONCENTRATIONS (2002)  
derived from MODIS satellite instrument data

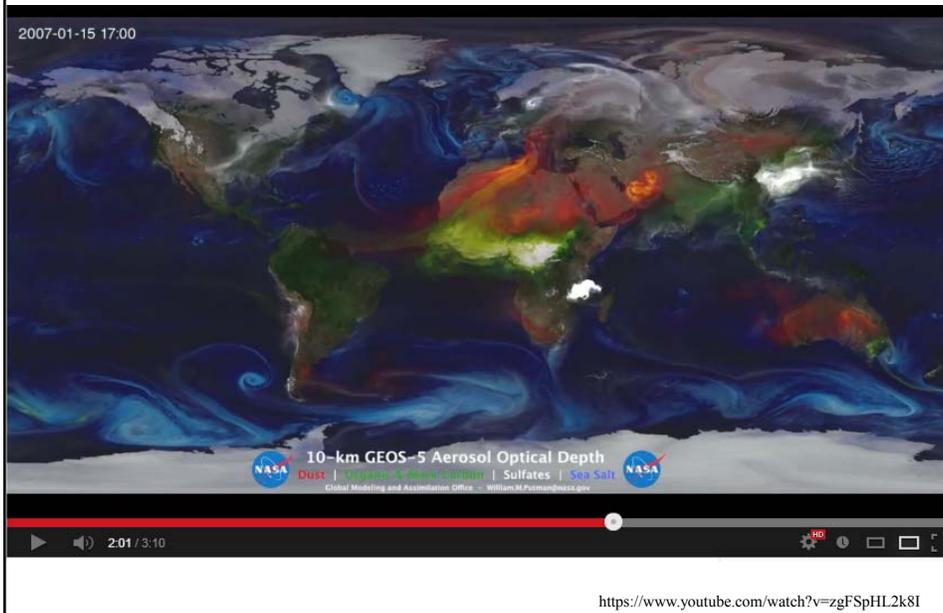


Clicker Q: How does the mass conc. of PM compare to other species?

- A. Similar to CO<sub>2</sub>
- B. Similar to CH<sub>4</sub>
- C. Similar to O<sub>3</sub>
- D. Similar to OH
- E. I don't know

Adapted from Jacob

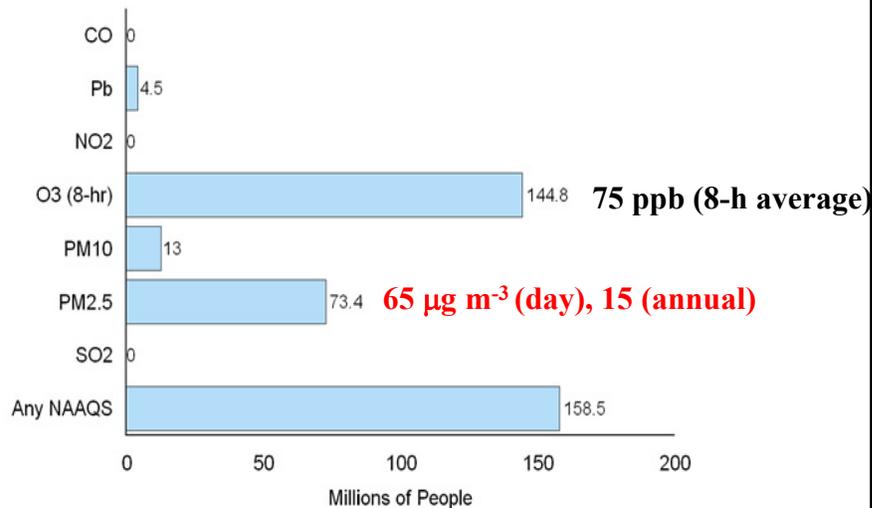
## Global Hi-Res Aerosol Simulation



<https://www.youtube.com/watch?v=zgFSpHL2k8I>

# Ozone and Particulate Matter (PM)

# millions of people living in areas exceeding national ambient air quality standards (NAAQS) in 2007



From Jacob

## Effects of Atmospheric Aerosols

- Health effects:
  - Epidemiological evidence: affect cardiorespiratory system, cause cancer, impair lung development of children
  - More deadly than car accidents (est. kills ~ 60,000 people / year in US)
- Ecological hazards:
  - Acid and nutrient deposition: damage ecosystems and ecological components, disturb nutrient balance
- Influence atmospheric chemistry:
  - Reaction media
  - Heterogeneous & surface rxns (e.g., *polar stratospheric clouds and the ozone*)
  - Transport media

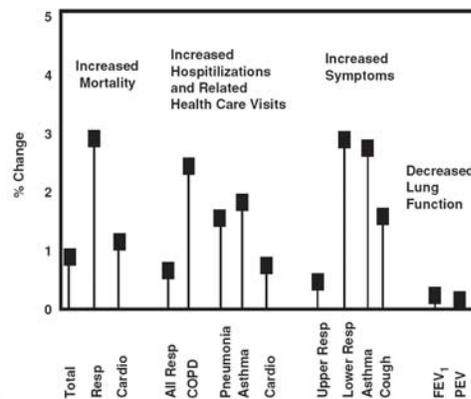


Figure 2.5. Stylized summary of acute exposure studies, percent change in health endpoint per 10 µg/m<sup>3</sup> increase in PM<sub>10</sub>. (Adapted from Pope and Dockery, 1999).

2005 INAAQS ASSESSMENT

From Zhang

# Size Distributions of Atmospheric Aerosols

## Why PM size matters?

- Particle toxicity (deposition efficiency are size dependent)
- Light scattering (0.1 – 1  $\mu\text{m}$  most efficient for scattering solar radiation)
- Surface rxns (w/ same PM mass, smaller particles higher total surface area)

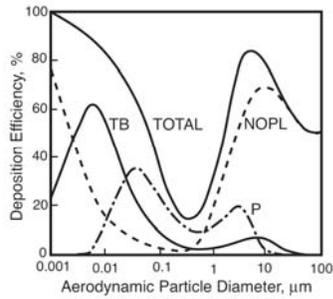


Figure 2.3. Particle deposition in the major regions of the human respiratory tract during normal respiration corrected for size dependent inhalability. (NOPL, naso-oro-pharyngo-laryngea) region; TB, tracheo-bronchial region; and P, pulmonary region). Developed from the National Council on Radiation Protection Model (NCRP, 1997) by Phalen (2002). 2003 NARSTO Assessment

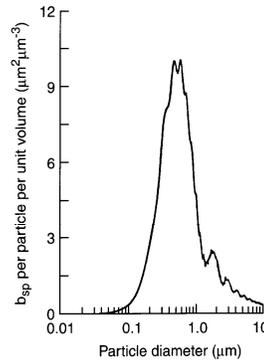
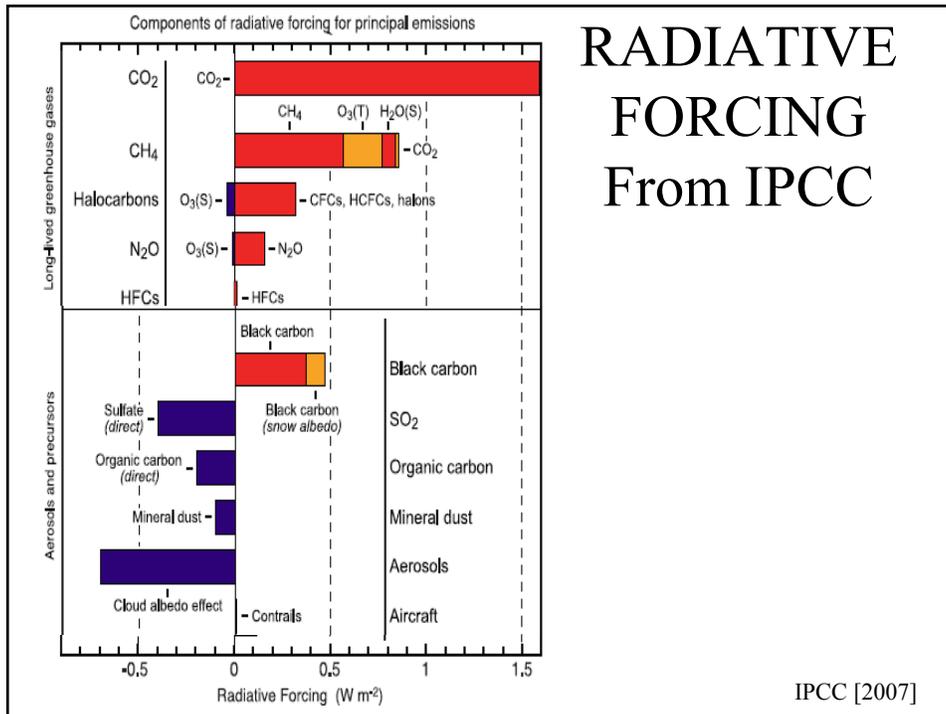


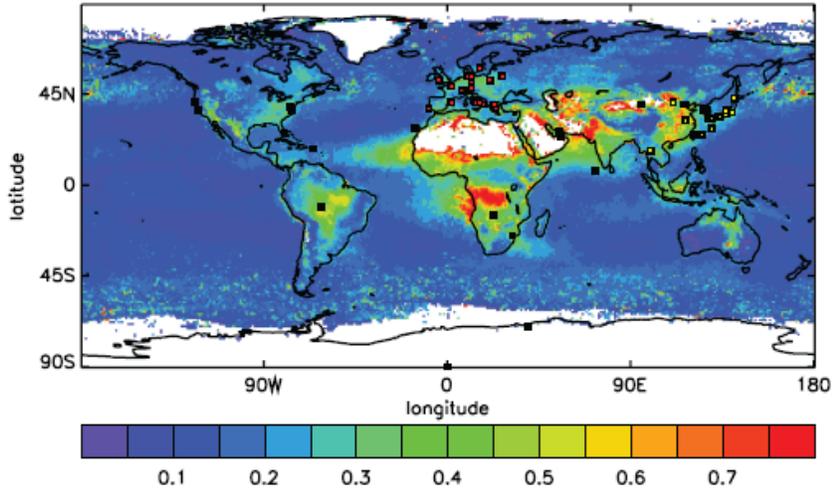
FIGURE 9.22 Scattering coefficient per particle divided by particle volume plotted as a function of diameter. The particles are assumed to be spheres of refractive index 1.50 and the light has  $\lambda = 550 \text{ nm}$  (adapted from Waggoner and Charlson, 1976). Finlayson-Pitts & Pitts

From Zhang



# AEROSOL OPTICAL DEPTH

August to October 2001

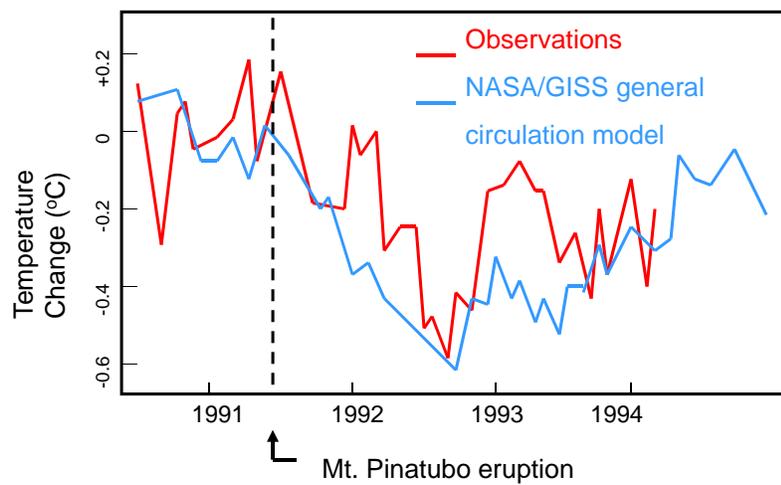


Global mean AOD is about 0.1, with 25% of that anthropogenic

From Jacob IPCC [2007]

# Evidence of Aerosol Effects on Climate

Temperature decrease following large volcanic eruptions



From Jacob

# Scattering vs. Absorbing Aerosols

Scattering sulfate and organic aerosol over Massachusetts



Partly absorbing dust aerosol downwind of Sahara

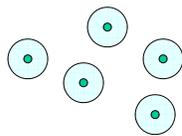


Absorbing aerosols (black carbon, dust) warm the climate by absorbing solar radiation

From Jacob

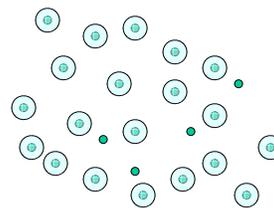
## Aerosol “Indirect Effect” from Cloud Changes

Clouds form by condensation on preexisting aerosol particles (“cloud condensation nuclei”)when  $RH > 100\%$



clean cloud (few particles):

- large cloud droplets
- efficient precipitation



polluted cloud (many particles):

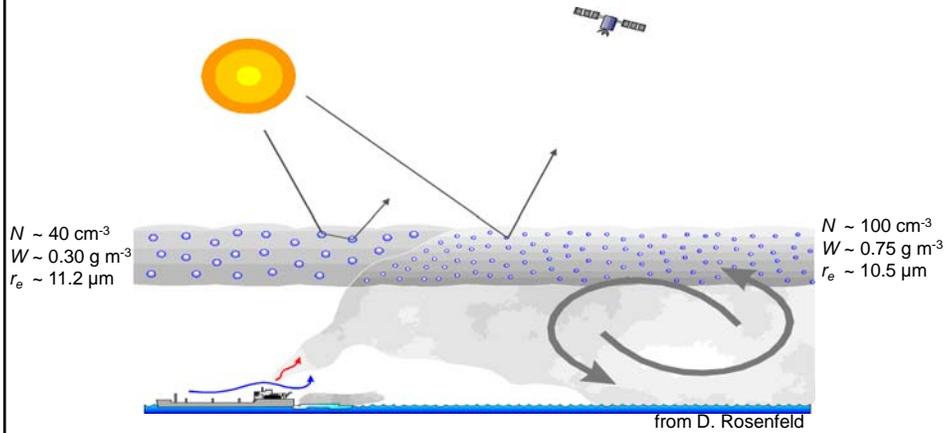
- small cloud droplets
- suppressed precipitation

Clicker Q: Based on slide 7, the clean cloud will be:

- A. More efficient in reflecting visible radiation back to space
- B. Less efficient
- C. Same efficiency
- D. It depends on additional information
- E. I don't know

Adapted from Jacob

## Evidence of Indirect Effect: Ship Tracks



- Particles emitted by ships increase concentration of cloud condensation nuclei (CCN)
- Increased CCN increase concentration of cloud droplets and reduce their avg. size
- Increased concentration and smaller particles reduce production of drizzle
- Liquid water content increases because loss of drizzle particles is suppressed
- Clouds are *optically thicker* and brighter along ship track

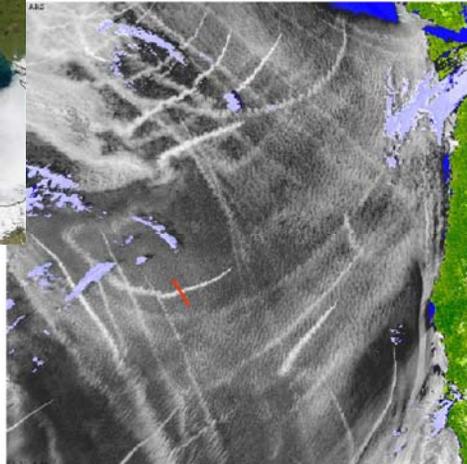
From Jacob

## Satellite Images of Ship Tracks



NASA, 2002  
Atlantic, France, Spain

AVHRR, 27. Sept. 1987, 22:45 GMT  
US-west coast

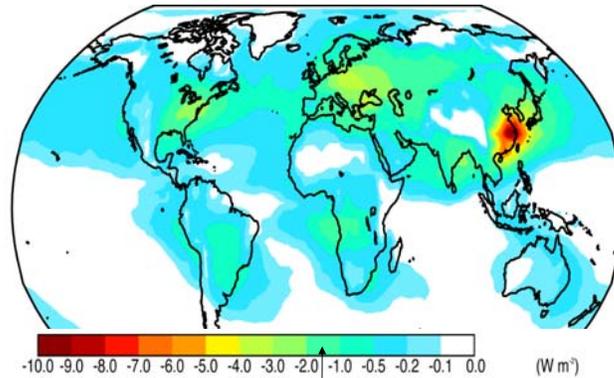


From Jacob

## Radiative forcing by aerosols is very inhomogeneous

...in contrast to the long-lived greenhouse gases

Present-day annual direct radiative forcing from anthropogenic aerosols



Leibensperger et al., 2011

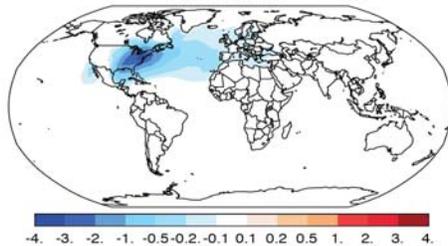
global radiative forcing from CO<sub>2</sub> (W m<sup>-2</sup>)

- Aerosol radiative forcing over polluted continents can more than offset forcing from greenhouse gases
- The extent to which this regional radiative forcing translates into regional climate response is not understood

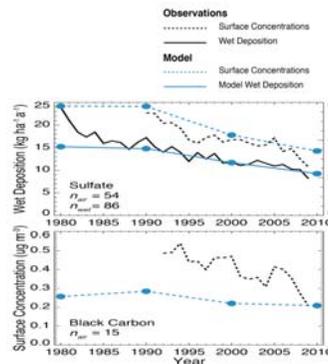
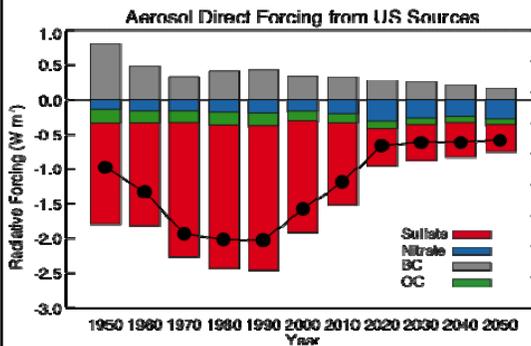
From Jacob

## Radiative forcing from US anthropogenic aerosol

Aerosol Direct Radiative Forcing - U.S. Sources (W m<sup>-2</sup>) - 2000  
Internal Mixture -0.05



- Forcing is mostly from sulfate, peaked in 1970-1990
- Little leverage to be had from BC control



Leibensperger et al., 2011

From Jacob

# Knudsen Number (Kn)

$$Kn = \frac{\lambda_{gas}}{R_p} = \frac{2\lambda_{gas}}{D_p}$$

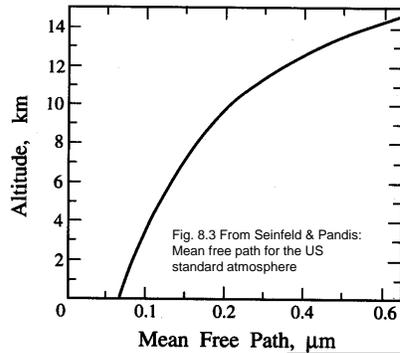
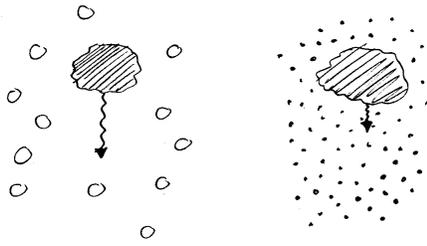
If a particle is sufficiently large, the gas surrounding it can be regarded as a continuous medium with a certain viscosity

A good figure of merit is Knudsen number (= mean free path,  $\lambda_{gas}$ , relative to the particle radius,  $R_p$ ):

- ✓  $Kn \gg 1 \Rightarrow$  kinetic regime (or free-molecular regime)
- ✓  $Kn \ll 1 \Rightarrow$  continuum regime (or viscous regime)

Solve in class: calculate Knudsen number for a particle with 2  $\mu\text{m}$  diameter in air at 1 atm

In a continuum regime, moving particle experiences friction against gas all the time, whereas in kinetic regime the particle can slip past molecules as if it is in vacuum



From Nidkorodov

# Stokes' Law

Particle moving with speed  $v$  in a continuous medium ( $Kn \ll 1$ ) with viscosity  $\eta$  experiences a drag force given by Stokes law

In molecular regime, Stokes law can still be applied with a slip correction factor,  $C_c$  (also known as Cunningham factor)

Stokes law can be used to predict the terminal speed of motion of a particle under the influence of a constant force (e.g., gravity)



Continuum regime:

$$F_{drag} = 6\pi\eta R_p v$$

Molecular regime:

$$F_{drag} = \frac{6\pi\eta R_p v}{C_c}$$

TABLE 8.3 Slip Correction Factor  $C_c$  for Spherical Particles in Air at 298 K and 1 atm

| $D_p$ ( $\mu\text{m}$ ) | $C_c$  |
|-------------------------|--------|
| 0.001                   | 216    |
| 0.002                   | 108    |
| 0.005                   | 43.6   |
| 0.01                    | 22.2   |
| 0.02                    | 11.4   |
| 0.05                    | 4.95   |
| 0.1                     | 2.85   |
| 0.2                     | 1.865  |
| 0.5                     | 1.326  |
| 1.0                     | 1.164  |
| 2.0                     | 1.082  |
| 5.0                     | 1.032  |
| 10.0                    | 1.016  |
| 20.0                    | 1.008  |
| 50.0                    | 1.003  |
| 100.0                   | 1.0016 |

$\eta$ : gas viscosity  
 $= 2 \times 10^{-5} \text{ kg / m/s}$  (air @ 300K)  
 $v$ : speed

Solve in class: Calculate sedimentation velocity of a 2  $\mu\text{m}$  diameter particle with a unit density at STP

From Nidkorodov

# Atmospheric Aerosols II

*Required reading: Jacob Chapter 8*

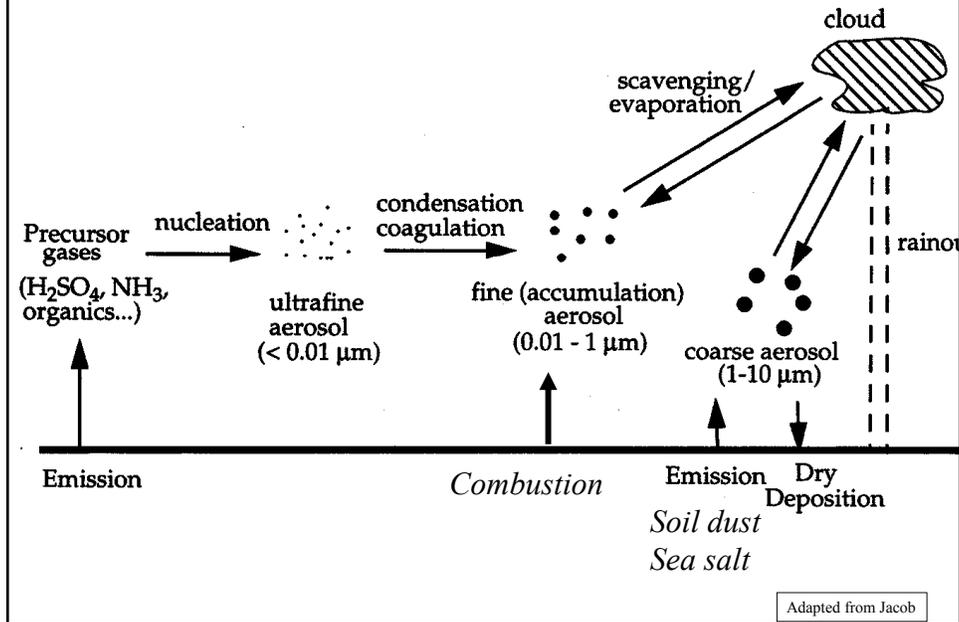
Atmospheric chemistry  
ATOC-5151 / CHEM-5151  
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## Review Question

- If an organic molecule with an IR absorption spectrum similar to that of methane partitions to the aerosol, its impact on radiative forcing will be on average:
  - A. The same as if it stayed in the gas phase
  - B. x1000 smaller
  - C. x3 larger
  - D. x1000 larger
  - E. I don't know

# Origin of the atmospheric aerosol



## Brownian Diffusion

- Small enough particles start to behave like gases and diffuse

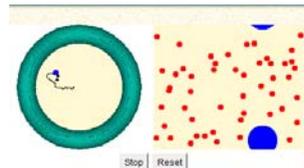
- Fick's law: 
$$J = -D \frac{dN}{dx}$$
  - $J$ : flux of particles
  - $D$ : diffusion coefficient
  - $N$ : number of particles

- Diffusion coefficient for particles: 
$$D = \frac{kTC}{3\pi\eta d}$$
  - $k$ : Boltzmann constant
  - $T$ : temperature
  - $C$ : Cunningham slip correction factor
  - $\eta$ : gas viscosity
  - $d$ : particle diameter

- Time scale for diffusion (D has units of m<sup>2</sup>/s): 
$$\tau_d \sim \frac{L^2}{D}$$
- Clicker Q:  $D = 6.9 \times 10^{-10} \text{ m}^2/\text{s}$  for a 100 nm particle. How quickly will it diffuse to the ground if it starts 1m above it?

- A. 1 s      B. 1 hr      C. 1 month  
D. 1 century      E. Dunno

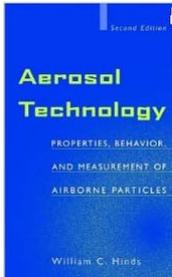
$$D_{\text{air}} \sim 10^{-5} \text{ m}^2/\text{s}$$



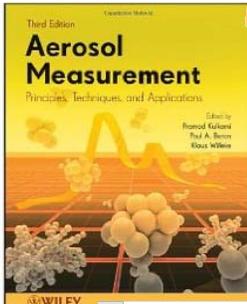
<http://www.aip.org/history/einstein/brownian.htm>

# Practical Aerosol Resources

Great intro to medium book



Measurement "bible"



- For practical aerosol calculations

- Aerosol calculator from Willeke and Baron
- Linked on course page

|     |   |             |  |                   |
|-----|---|-------------|--|-------------------|
| 116 |   |             |  |                   |
| 117 | Diffusion coefficient (B&W 4-12; W&B 3-12; Hinds 2-35, 7-7) |             | mechanical mobility (B&W 4-14; W&B 3-14; |                   |
| 118 | Temperature   | 293.15      | Kelvin                                   |                   |
| 119 | Pressure  | 101.3       | kPa                                      |                   |
| 120 | Molecular weight  | 0.02896     | kg/mole                                  | = 0.02896 for air |
| 121 | Particle/molecule diameter                                  | 4           | µm                                       |                   |
| 122 | Particle density  | 1000        | kg/m <sup>3</sup>                        |                   |
| 123 | -----   |             |  |                   |
| 124 | Air viscosity =   | 1.80711E-05 | Pa*s                                     |                   |
| 125 | Slip correction factor =                                    | 1.04148201  |  |                   |
| 126 | Diffusion coefficient =                                     | 1.51E-13    | m <sup>2</sup> /s                        | molecular range   |
| 127 | Diffusion coefficient =                                     | 6.18E-12    | m <sup>2</sup> /s                        | particle range    |
| 128 | Mechanical mobility =                                       | 1.53E+09    | m/(N*s)                                  |                   |
| 129 | Mean thermal velocity =                                     | 0.000554454 | m/s                                      |                   |
| 130 |   |             |  |                   |
| 131 | -----   |             |  |                   |

## Sedimentation vs. Brownian Diffusion

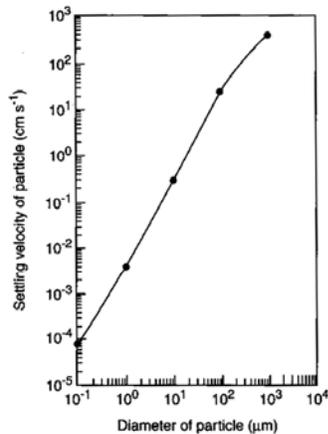


FIGURE 9.16 Settling velocities in still air at 0°C and 760 Torr pressure for particles having a density of 1 g cm<sup>-3</sup> as a function of particle diameter. For spherical particles of unit density suspended in air near sea level, the Stokes law applies over a considerable range of particle sizes, where the line is straight, but a correction is required at the particle size extremes (adapted from LBL, 1979).

TABLE 9.5 Cumulative Deposition of Unit Density Particles onto a Horizontal Surface from Unit Aerosol Concentrations<sup>a</sup> during 100 s by Diffusion and Gravitational Settling<sup>b</sup>

| Diameter (µm) | Cumulative deposition                |                                     | Ratio diffusion/settling |
|---------------|--------------------------------------|-------------------------------------|--------------------------|
|               | Diffusion (number cm <sup>-2</sup> ) | Settling (number cm <sup>-2</sup> ) |                          |
| 0.001         | 2.5                                  | 6.5 × 10 <sup>-5</sup>              | 3.8 × 10 <sup>4</sup>    |
| 0.01          | 0.26                                 | 6.7 × 10 <sup>-4</sup>              | 390                      |
| 0.1           | 2.9 × 10 <sup>-2</sup>               | 8.5 × 10 <sup>-3</sup>              | 3.4                      |
| 1.0           | 5.9 × 10 <sup>-3</sup>               | 0.35                                | 1.7 × 10 <sup>-2</sup>   |
| 10            | 1.7 × 10 <sup>-3</sup>               | 31                                  | 5.5 × 10 <sup>-5</sup>   |
| 100           | 5.5 × 10 <sup>-4</sup>               | 2500                                | 2.2 × 10 <sup>-7</sup>   |

<sup>a</sup> This assumes an aerosol concentration of 1 particle cm<sup>-3</sup> outside the gradient region.

<sup>b</sup> From Hinds (1982).

- ✓ Collisions with molecules exert randomly oriented forces on the particle resulting in its chaotic Brownian motion that competes with sedimentation under gravity
- ✓ Brownian motion wins for particles < 0.1 µm
- ✓ In the absence of convection, particles larger than 100 µm will quickly sediment from the troposphere (they drop like rocks!)

Question: size of maximum lifetime is the size as max effect on climate and human health. Is this a coincidence or is there a reason why they are the same? A. Coincidence B. Reason C. I don't know

From Nidkorodov

# Dry Deposition Velocity

$$J_{dd} = v_{dep} C$$

$J_{dd}$ : dry deposition flux of particles ( $\text{p}/\text{cm}^2 \text{ s}^{-1}$ )  
 $v_{dep}$ : "deposition velocity" ( $\text{cm}/\text{s}$ )  
 $C$ : particle concentration ( $\text{cm}^{-3}$ )

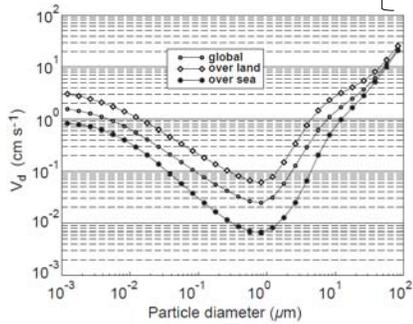


Fig. 1. Annual mean deposition velocities by particle size and surface type (particle density  $1000 \text{ kg m}^{-3}$ ).

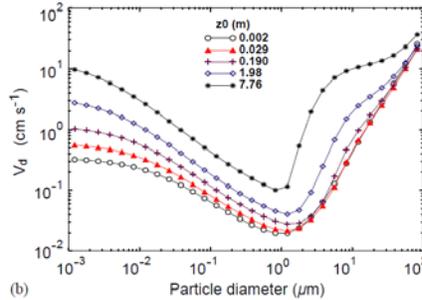
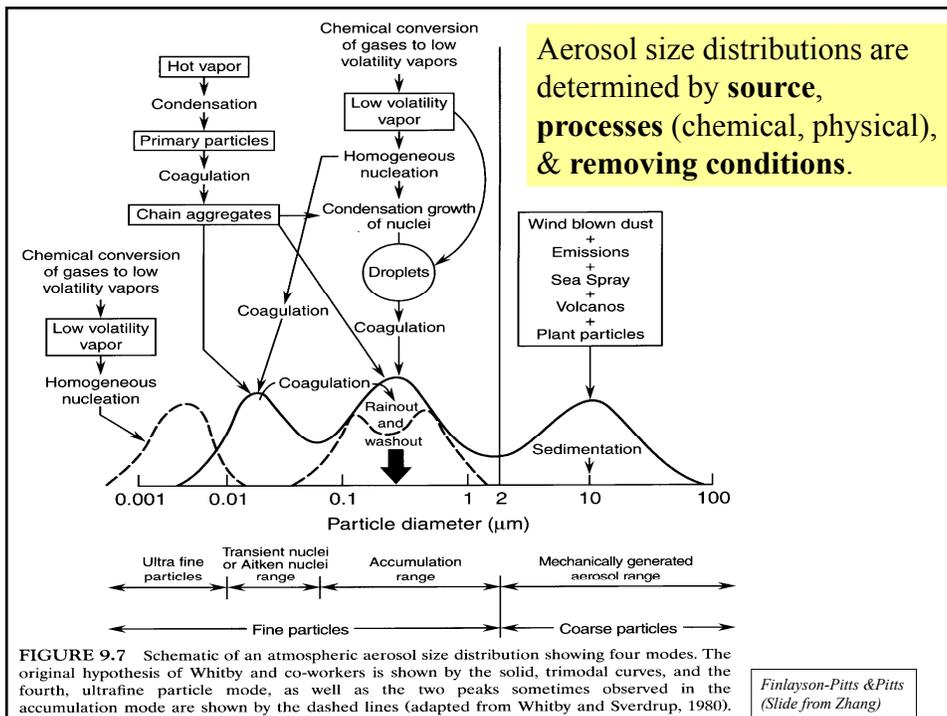


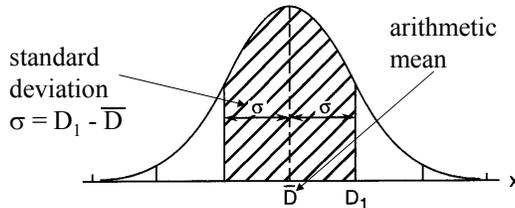
Fig. 6. Effect of surface roughness on deposition velocity: (a) unstable and (b) stable and neutral cases (particle density  $1000 \text{ kg m}^{-3}$ ).

- Clicker Q: timescale of loss of 100 nm from a 1 km boundary layer over a forest?
- A. 100 s
  - B. 1 hr
  - C. 1 day
  - D. 1 century
  - E. I don't know



# Mathematical Description of Size Distributions

Normal distribution (bell shaped)



- A normal distribution is fully characterized by the  $\bar{D}$  and the  $\sigma$
- 68% of the particles have sizes in the range of  $\bar{D} \pm \sigma$

FIGURE 9.12 Meaning of standard deviation for a normal distribution. The hatched area represents 68% of total area under curve.

*Finlayson-Pitts & Pitts*

The size distributions of atmospheric aerosols are best described by lognormal distributions (i.e., the logarithm of particle sizes is normally distributed).

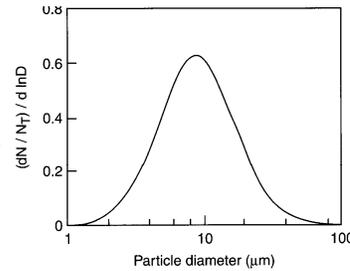
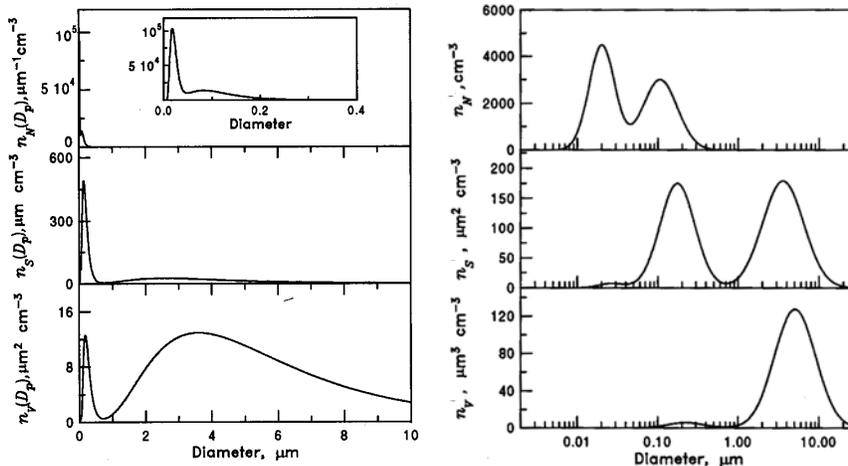


FIGURE 9.13 Frequency distribution curve (logarithmic size scale) (adapted from Hinds, 1982). *Finlayson-Pitts & Pitts*

## Relating Particle Size Distributions



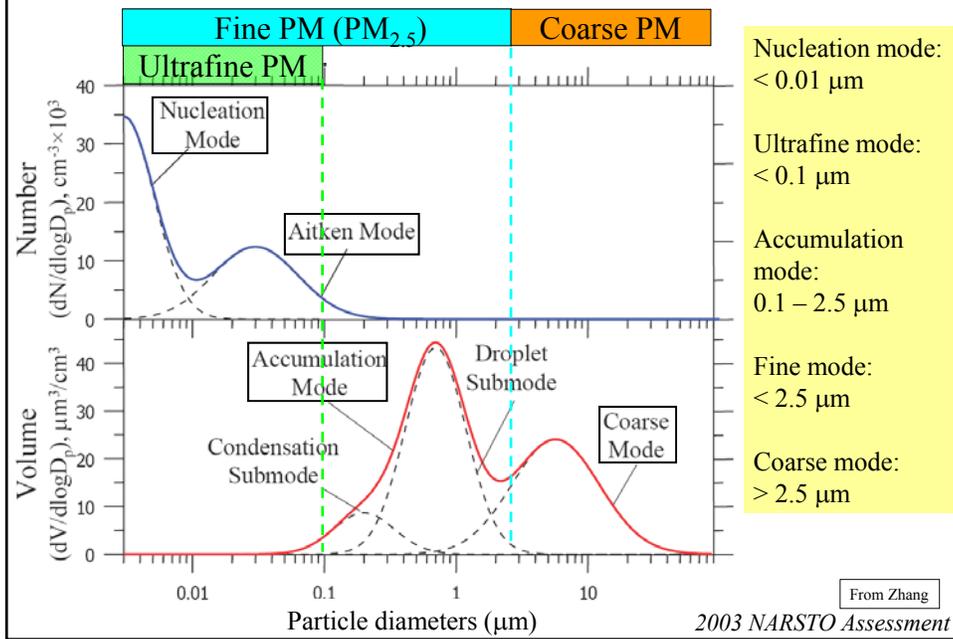
Note: these are several representations of one and the same distribution!

$$\log x/y = \log x - \log y$$

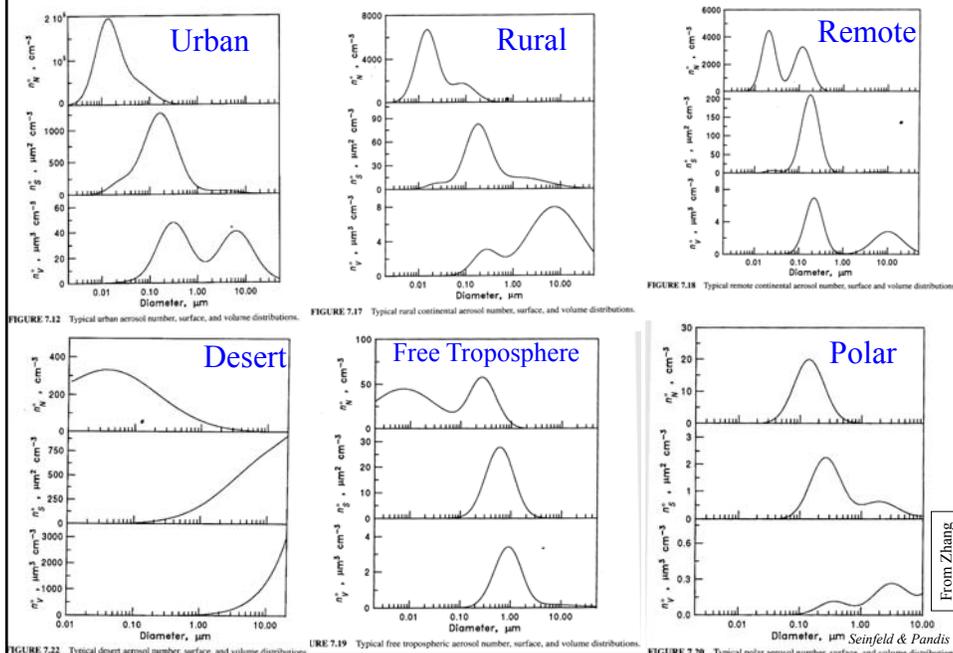
Solve in class: Based on the distributions shown above, how many particles have diameter = 0.1  $\mu\text{m}$ ?  
 How many particles have diameters in the range 0.1 to 0.11  $\mu\text{m}$ ? Use both  $n_N(D_p)$  and  $n_N^e(D_p)$  to find your answers.

From Nidkorodov

# Size Distribution of Ambient Aerosols: Modes



# Typical PM Size Distributions in Various Atmospheres



## Clicker Questions

- |   |   |
|---|---|
| <ul style="list-style-type: none"> <li>• The number of particles in the polar atmosphere below 1 micron is</li> <li style="margin-left: 20px;">A. <math>2 \text{ cm}^{-2}</math></li> <li style="margin-left: 20px;">B. <math>2 \text{ cm}^{-3}</math></li> <li style="margin-left: 20px;">C. <math>20 \text{ cm}^{-3}</math></li> <li style="margin-left: 20px;">D. <math>2000 \text{ cm}^{-3}</math></li> <li style="margin-left: 20px;">E. I don't know</li> </ul> | <ul style="list-style-type: none"> <li>• The typical mass of particles in the free troposphere below 200 nm is</li> <li style="margin-left: 20px;">A. <math>0.02 \mu\text{m}^3 \text{ cm}^{-3}</math></li> <li style="margin-left: 20px;">B. <math>0.2 \mu\text{m}^3 \text{ cm}^{-3}</math></li> <li style="margin-left: 20px;">C. <math>20 \mu\text{m}^3 \text{ cm}^{-3}</math></li> <li style="margin-left: 20px;">D. <math>200 \mu\text{m}^3 \text{ cm}^{-3}</math></li> <li style="margin-left: 20px;">E. I don't know</li> </ul> |
|---|---|

### Particle ~ Particle Interaction (Coagulation)

Coagulation: formation of a single particle via collision and sticking of two smaller particles (e.g., Brownian coagulation)

- Need to consider in the context of different regimes.
- Coagulation rate depends on:
  - Diameter of the large particle
  - Diffusion rates of the smaller particle
  - Concentration of the particles
- Smallest coagulation rates b/w particles of same size (i.e., self-coagulation slowest).

$$J_{12} = K_{12} N_1 N_2$$

**TABLE 12.3 Coagulation Coefficients ( $\text{cm}^3 \text{ s}^{-1}$ ) of Atmospheric Particles**

| $D_{p2}$ ( $\mu\text{m}$ ) | $D_{p1}$ ( $\mu\text{m}$ ) |                      |                       |                       |                       |                       |
|----------------------------|----------------------------|----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
|                            | 0.002                      | 0.01                 | 0.1                   | 1.0                   | 10                    | 20                    |
| 0.002                      | $4.5 \times 10^{-10}$      | $3 \times 10^{-9}$   | $1.6 \times 10^{-7}$  | $3.7 \times 10^{-6}$  | $4 \times 10^{-5}$    | $8 \times 10^{-5}$    |
| 0.01                       | $3 \times 10^{-9}$         | $9 \times 10^{-10}$  | $1.2 \times 10^{-8}$  | $1.6 \times 10^{-7}$  | $1.6 \times 10^{-6}$  | $3 \times 10^{-6}$    |
| 0.1                        | $1.6 \times 10^{-7}$       | $1.2 \times 10^{-8}$ | $7.2 \times 10^{-10}$ | $2.4 \times 10^{-9}$  | $2.2 \times 10^{-8}$  | $4.3 \times 10^{-8}$  |
| 1                          | $3.7 \times 10^{-6}$       | $1.6 \times 10^{-7}$ | $2.4 \times 10^{-9}$  | $3.4 \times 10^{-10}$ | $1.0 \times 10^{-9}$  | $1.9 \times 10^{-9}$  |
| 10                         | $4 \times 10^{-5}$         | $1.6 \times 10^{-6}$ | $2.2 \times 10^{-8}$  | $1.0 \times 10^{-9}$  | $3 \times 10^{-10}$   | $3.3 \times 10^{-10}$ |
| 20                         | $8 \times 10^{-5}$         | $3.0 \times 10^{-6}$ | $4.3 \times 10^{-8}$  | $1.9 \times 10^{-9}$  | $3.3 \times 10^{-10}$ | $3 \times 10^{-10}$   |

Adapted from Zhang

## Particle ~ Particle Interaction (Coagulation)

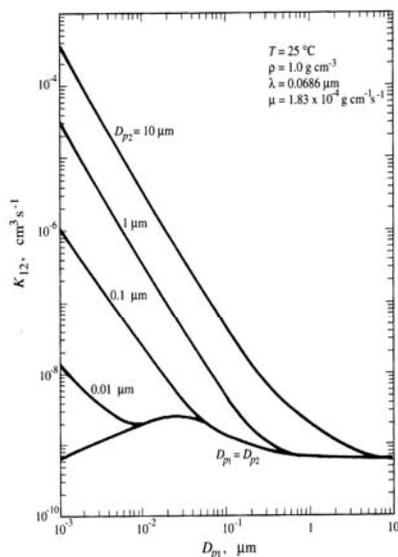


FIGURE 12.5 Brownian coagulation coefficient  $K_{12}$  for coagulation in air at 25°C of particles of diameters  $D_{p1}$  and  $D_{p2}$ . The curves were calculated using the correlation of Fuchs in Table 12.1. To use this figure find the *smaller* of the two particles as the abscissa and then locate the line corresponding to the larger particle.  
From Seinfeld and Pandis

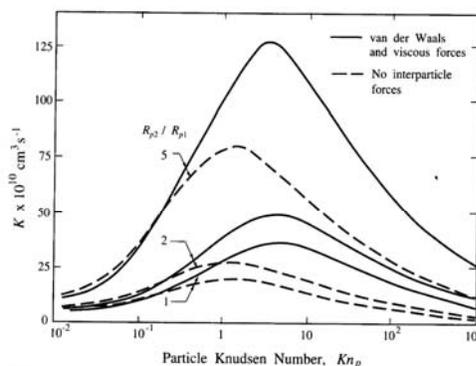


FIGURE 12.10 Coagulation coefficient at 300 K,  $\rho_p = 1 \text{ g cm}^{-3}$ ,  $A/kT = 20$  as a function of Knudsen number ( $Kn_p$ ) for particle radii ratios of 1, 2, and 5 both in the presence and in the absence of interparticle forces.  
From Seinfeld & Pandis

Bigger size ratio ( $D_{p1}/D_{p2}$ ),  
higher coagulation rates  
(Pandis' "The elephant and the ant")

Adapted from Zhang

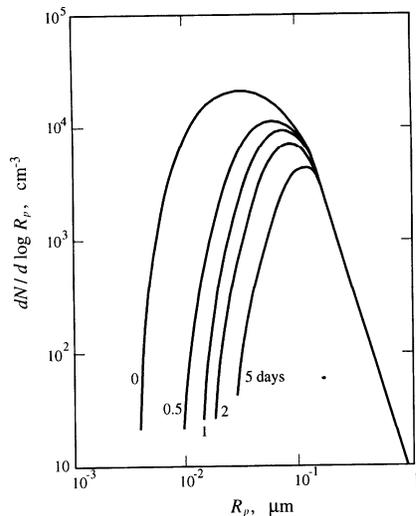
## Clicker Q on Coagulation

- $N_{100\text{nm}} = 1000 \text{ cm}^{-3}$  and  $N_{1\text{nm}} = 10^6 \text{ cm}^{-3}$
- This is typical of new particle formation events in the atmosphere
- What is the timescale for loss of 1 nm particles to coagulation to 100 nm particles?

- 1 s
- 1000 s
- 1 hr
- 3.2 days
- I don't know

Followup: what is the timescale for the 100 nm particles?

## How Does Coagulation Affect Size Distribution?



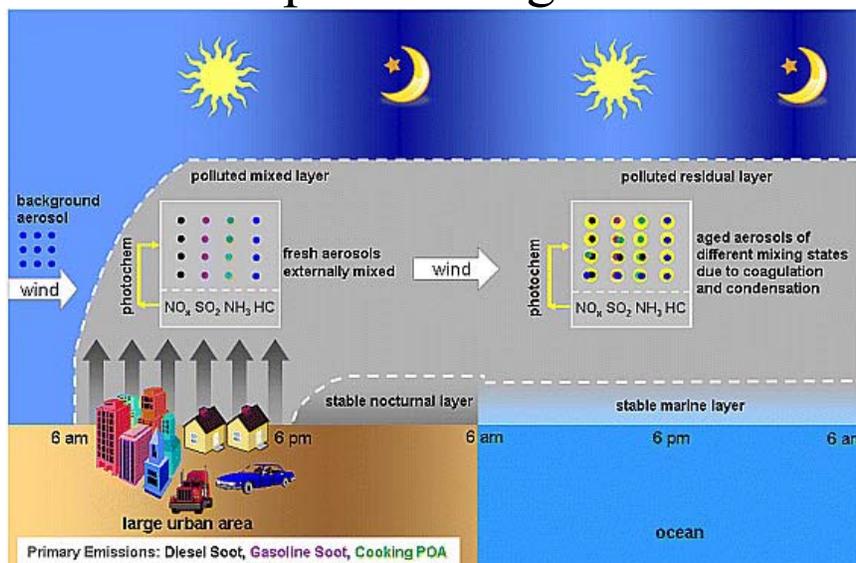
- Small particles faster Brownian motion  $\rightarrow$  more collision  $\rightarrow$  faster coagulation loss.
- Coagulation dramatically affects the # conc. of particles w/  $D_p < 0.05 \mu\text{m}$

FIGURE 12.13 Evolution of a coagulating particle population size distribution during a period of 5 days (Butcher and Charlson, 1972).

From Seinfeld and Pandis

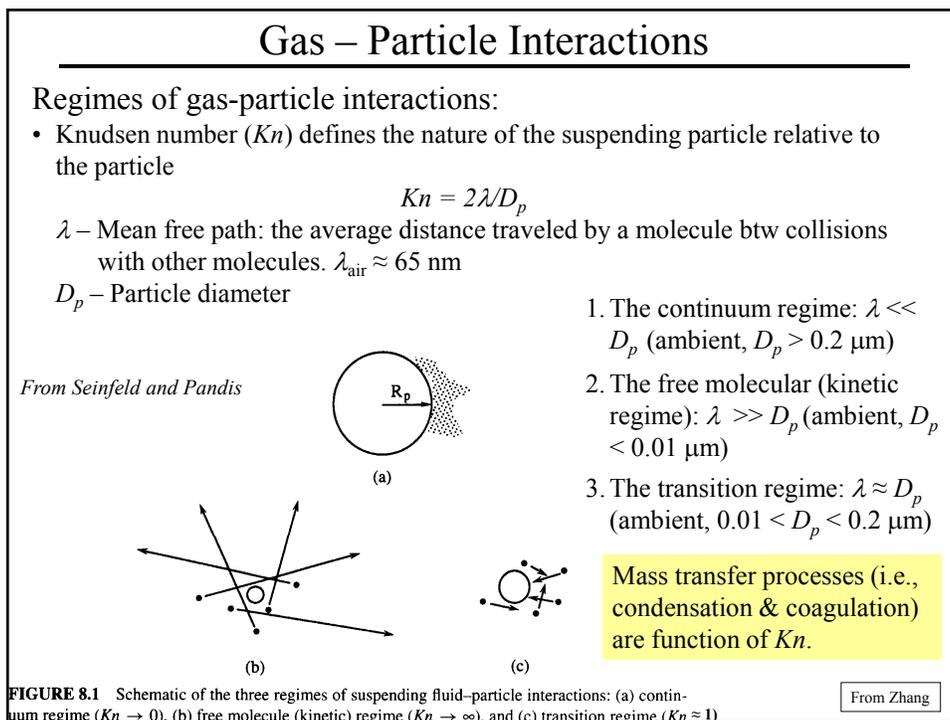
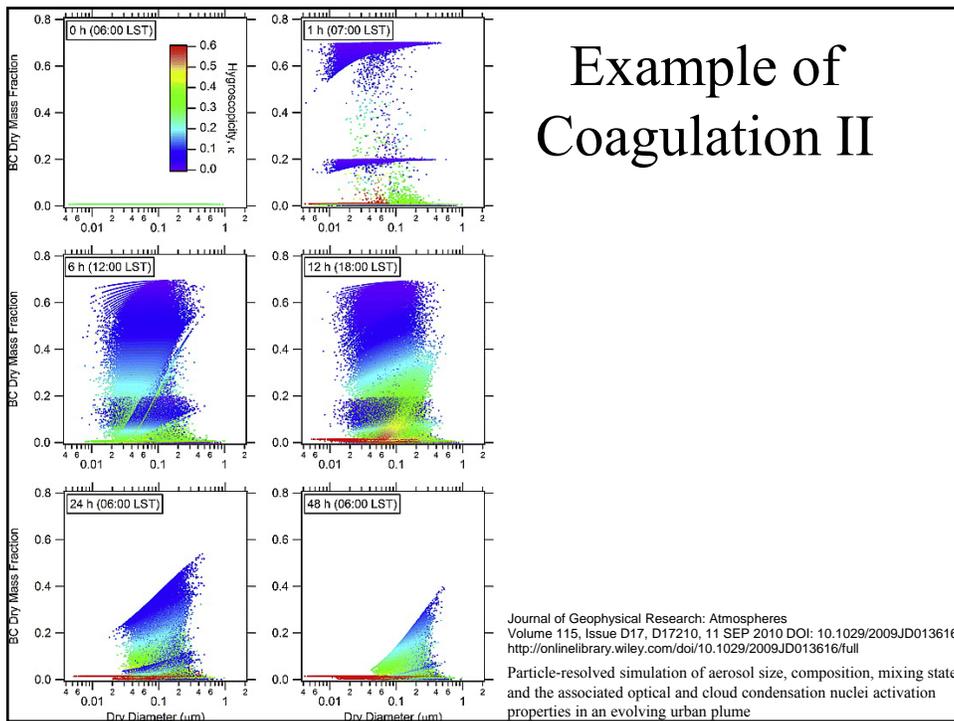
From Zhang

## Example of Coagulation I



Journal of Geophysical Research: Atmospheres  
Volume 115, Issue D17, D17210, 11 SEP 2010 DOI: 10.1029/2009JD013616  
<http://onlinelibrary.wiley.com/doi/10.1029/2009JD013616/full#jgrd16283-fig-0001>

Particle-resolved simulation of aerosol size, composition, mixing state and the associated optical and cloud condensation nuclei activation properties in an evolving urban plume



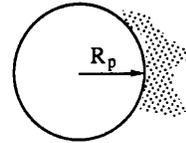
## Gas to Particle Conversions

Mass transfer of gas molecules to particles (i.e., condensation):

- $J_c$ : the total flow of A(g) (moles time<sup>-1</sup>) toward the particle in **continuum regime**

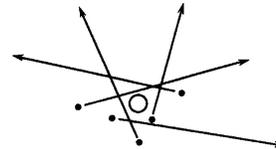
$$J_c = 4\pi R_p D_g (c_\infty - c_s)$$

- $R_p$ : Particle radius
- $D_g$ : Diffusivity of gas A
- $c_\infty$ : Conc. of A far from the particle
- $c_s$ : Vapor phase conc. of A at the particle surface



- $J_k$ : the total flow of A(g) (moles time<sup>-1</sup>) toward the particle in **free molecular (kinetic regime)**

$$J_k = \pi R_p^2 \bar{c}_A \alpha (c_\infty - c_s); \quad \bar{c}_A = \left( \frac{8kT}{\pi m_A} \right)^{1/2}$$



- $\bar{c}_A$ : Mean speed of the molecules
- $\alpha$ : Molecular accommodation coefficient, i.e., probability of A to stick on particle.  
 $0 \leq \alpha \leq 1$

From Zhang

## Gas to Particle Conversions (Mass Transfer)

Mass transfer of gas molecules to particles (i.e., condensation):

- $J$ : the total flow of A(g) (moles time<sup>-1</sup>) toward the particle in **transition regime**
  - $J_c$  &  $J_k$  eqns are not valid when  $\lambda \approx D_p$  (or  $Kn \approx 1$ )
  - No general solution exists from solving distribution of gas molecules
  - ➔ Use flux matching to determine  $J$

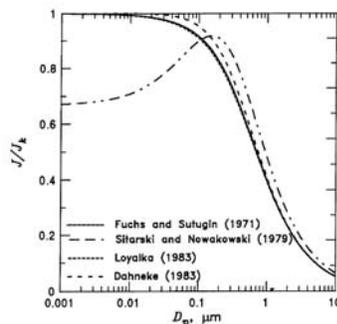


FIGURE 11.2 Mass transfer rate predictions for the transition regime by the approaches of (a) Fuchs and Sutugin, (b) Dahneke, (c) Loyalka and (d) Sitariski and Nowakowski ( $z = 15$ ) as a function of particle diameter. Accommodation coefficient  $\alpha = 1$ .

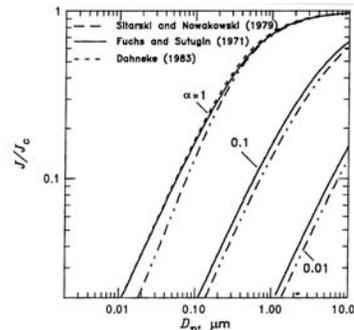


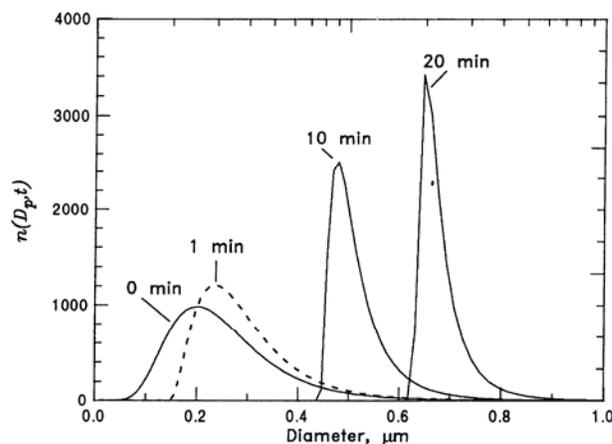
FIGURE 11.4 Mass transfer rates as a function of particle diameter for accommodation coefficients values 1.0, 0.1, and 0.01 for the approaches of Sitariski and Nowakowski (1979), Fuchs and Sutugin (1970), and Dahneke (1983).

From Seinfeld and Pandis

From Zhang

## How Does Condensation Affect Size Distribution?

- Condensation/Evaporation  $\rightarrow D_p$  change & size dist. change shape.
- Under condensation, smaller particles grow much faster than larger ones  $\rightarrow$  The size distribution becomes much narrower



**FIGURE 12.3** Evolution of a log-normal distribution (initially  $\bar{D}_p = 0.2 \mu\text{m}$ ,  $\sigma_g = 1.5$ ) assuming  $D_i = 0.1 \text{ cm}^2 \text{ s}^{-1}$ ,  $M_i = 100 \text{ g mol}^{-1}$ ,  $(p_i - p_{eq}) = 10^{-9} \text{ atm}$  (1 ppb),  $T = 298 \text{ K}$  and  $\rho_p = 1 \text{ g cm}^{-3}$ .

From Seinfeld and Pandis

From Zhang

## Condensation vs. Coagulation Rates

TABLE 9.10 Typical Time Scales for Various Aerosol Fates<sup>a</sup>

| Fate  | Type of air mass |               |                   |                      |
|---|------------------|---------------|-------------------|----------------------|
|   | Urban            | Remote marine | Free troposphere  | Nonurban continental |
| Condensation  | 0.01–1 h         | 1–10 h        | 2–20 h            | 0.5–20 h             |
| Coagulation of 0.03- $\mu\text{m}$ -particles with larger particles | 0.1–2 days       | 10–30 days    | ~50 days          | 1–5 days             |
| Deposition  |                  |               |                   |                      |
| 0.03- $\mu\text{m}$ particles                                       | 0.5–10 days      | 0.5–10 days   | —                 | ~1 month             |
| 0.3- $\mu\text{m}$ particles  | ~1 month         | ~1 month      | —                 | ~1 month             |
| Transport   | 2–5 days         | 1–2 weeks     | 3 days to 2 weeks | 1–2 weeks            |

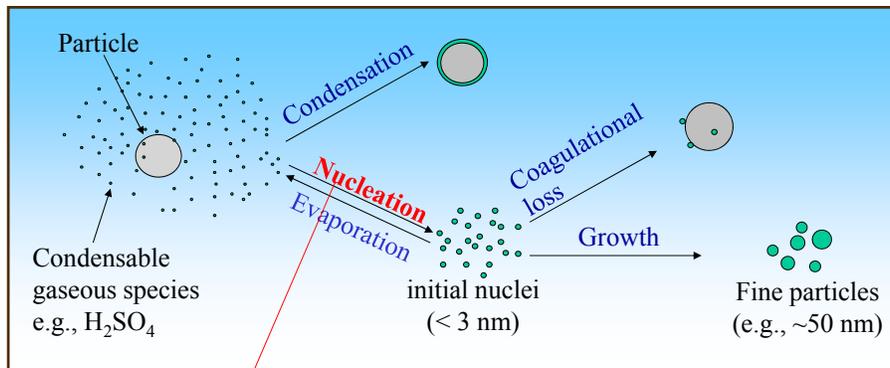
<sup>a</sup> From Pandis *et al.* (1995).

From Finlayson-Pitts and Pitts

- At ambient conditions, condensation faster than coagulation, except during new particle formation events

Adapted from Zhang

## Gas to Particle Conversions (Particle Nucleation)

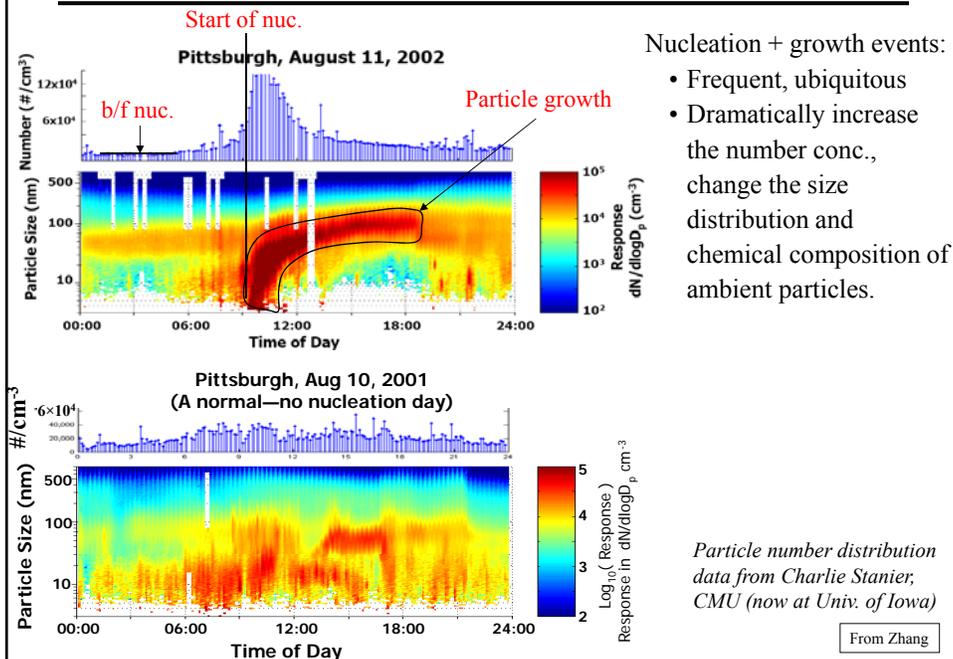


- Nucleation
- Condensation and nucleation are competing processes.
- Nucleation dominates when PM condensational sink is low.

- Possible nucleation mechanism
- Binary nucleation (H<sub>2</sub>SO<sub>4</sub> + H<sub>2</sub>O)
  - Ternary nucleation (H<sub>2</sub>SO<sub>4</sub> + NH<sub>3</sub> + H<sub>2</sub>O)
  - Organic compounds nucleation
  - Ion-induced nucleation

From Zhang

## How Does Nucleation Affect Size Distribution?



From Zhang

## Chemical Reactions of Particles

- Chemistry

- Solid aerosol provide surfaces upon which trace gases can be absorbed and then react
- Liquid aerosols absorb gases which may then react together in solution

e.g.  $\text{SO}_2 \rightarrow \text{H}_2\text{SO}_4$

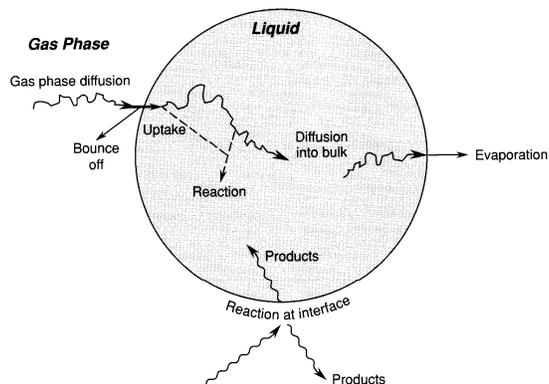
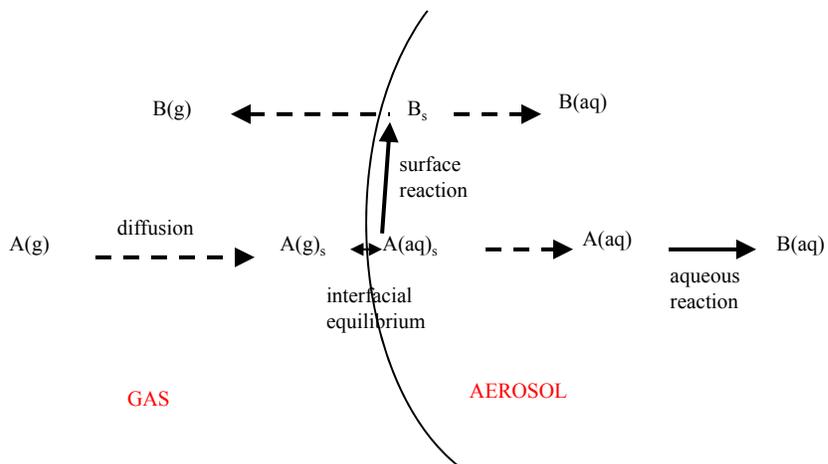


FIGURE 5.12 Schematic diagram of uptake and reaction of gases in liquids.

*From Finlayson-Pitts and Pitts*

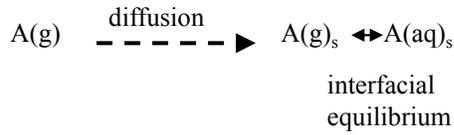
## GENERAL SCHEMATIC FOR HETEROGENEOUS CHEMISTRY



Aerosols enable surface and ionic reactions that would not happen in the gas phase; also concentrate low-volatility species in condensed phase

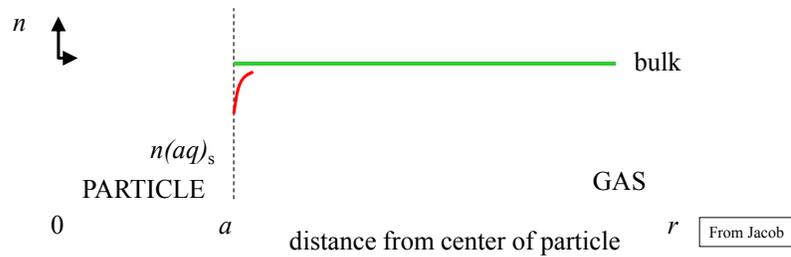
From Jacob

# FLUX AT THE GAS-PARTICLE INTERFACE

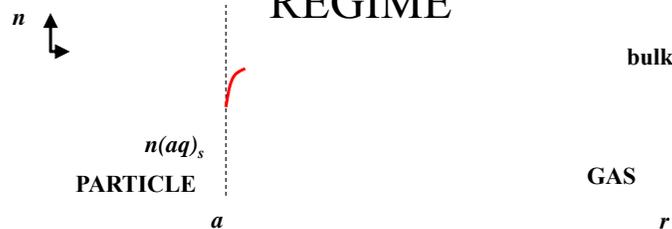


$l$  = mean free path of air (0.18  $\mu\text{m}$  at STP)  
 $a$  = particle radius  
 Knudsen number  $Kn = a/l$

$Kn \gg 1$ : continuum (diffusion-limited) regime  
 $Kn \ll 1$ : free molecular (collision-limited) regime



# SOLUTION FOR THE CONTINUUM REGIME



Continuity equation:

$$D \nabla^2 n_g(r) = 0 \quad \text{with BCs } n_g(\infty) = n_{bulk}, \quad n_g(a) = n_{aq}(a) / K_H$$

$D$  = molecular diffusion coefficient in gas phase

$K_H$  = Henry's law equilibrium constant

In spherical coordinates,

$$D \frac{1}{r^2} \frac{d}{dr} \left( r^2 \frac{dn_g}{dr} \right) = 0$$

Solve for the transfer flux at gas-particle interface:

$$F = -D \left. \frac{dn}{dr} \right|_{r=a} = \frac{D}{a} \left( n_g(\infty) - \frac{n_{aq}(a)}{K_H} \right)$$

From Jacob

## SOLUTION FOR THE FREE MOLECULAR REGIME

Collision flux with surface from random motion of molecules:

$$F = \frac{v}{4} \left( n_g - \frac{n_{aq}(a)}{K_H} \right)$$

where  $v$  is the mean molecular speed. Only a fraction  $\alpha$  (mass accommodation coefficient) of collisions results in bulk uptake by the particle, so the uptake flux is

$$F = \frac{\alpha v}{4} \left( n_g - \frac{n_{aq}(a)}{K_H} \right)$$

From Jacob

## APPROXIMATE SOLUTION FOR TRANSITION REGIME:

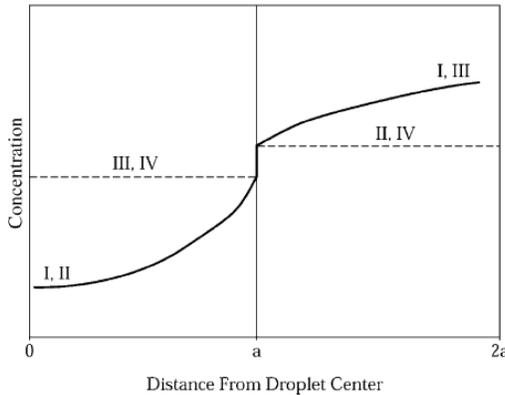
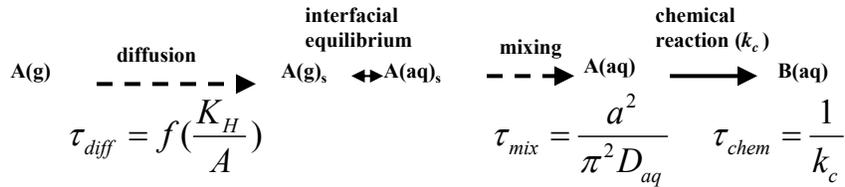
$$-\frac{dn_g(\infty)}{dt} = kA \left( n_g(\infty) - \frac{n_{aq}(a)}{K_H} \right)$$

where  $A$  is the aerosol surface area per unit volume of air ( $\text{cm}^2 \text{cm}^{-3}$ ), and  $k$  is a first-order gas-particle transfer rate constant:

$$k = \left( \frac{a}{D} + \frac{4}{\alpha v} \right)^{-1}$$

From Jacob

# TIME SCALES FOR GAS-PARTICLE TRANSFER



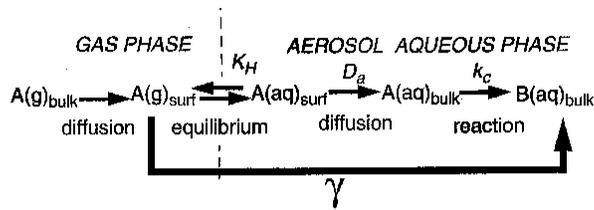
- In cloud:**
- CASE I:  $\tau_{chem} < \tau_{mix}, \tau_{chem} < \tau_{diff}$  **OH**
  - CASE II:  $\tau_{chem} < \tau_{mix}, \tau_{chem} > \tau_{diff}$  **O<sub>3</sub>, NO<sub>3</sub>**
  - CASE III:  $\tau_{chem} > \tau_{mix}, \tau_{chem} < \tau_{diff}$  **HO<sub>2</sub>**
  - CASE IV:  $\tau_{chem} > \tau_{mix}, \tau_{chem} > \tau_{diff}$  **most others; bulk equilibrium**

Jacob, Atmos. Environ. 2000

From Jacob

## REACTION PROBABILITY $\gamma$ : simplified representation of aerosol chemistry

$\gamma$  = probability that a gas molecule impacting the surface undergoes reaction



$\gamma$  convolves all transfer/reaction processes:

$$\gamma = \left[ \frac{1}{\alpha} + \frac{v}{4K_H RT \sqrt{D_a k_c}} \coth(q) - \frac{1}{q} \right]^{-1} \qquad q = a \sqrt{\frac{k_c}{D_a}} \text{ so that one can write}$$

$$-\frac{d[A(g)]}{dt} = k[A]$$

with

$$k = \frac{A}{\frac{a}{D_g} + \frac{4}{v\gamma}}$$

Jacob, Atmos. Environ. 2000

## How Do Chemical Reactions Affect Size Distribution?

Due to cloud processing of small mode PM

1. Agglomeration of smaller PM
2. Gas  $\rightarrow$  PM (e.g.,  $\text{SO}_2$  oxidation)

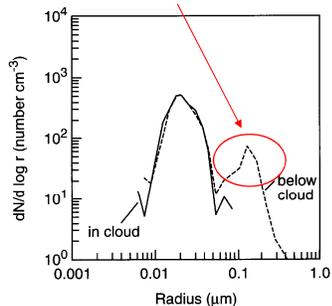
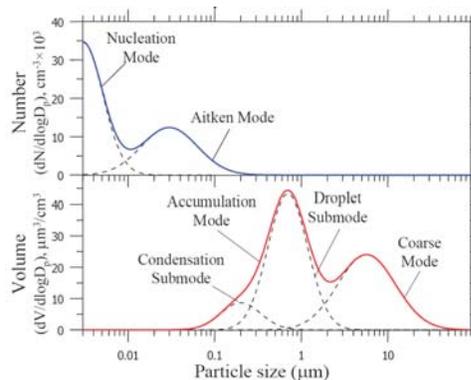


FIGURE 9.33 Size distribution of particles in clouds (solid line) and below the clouds (dashed line), showing two modes (adapted from Hoppel *et al.*, 1994). From Finlayson-Pitts & Pitts



**Aqueous reactions (in fog/cloud droplets) responsible for the bimodal distribution of the accumulation mode.**

## Vertical Variation

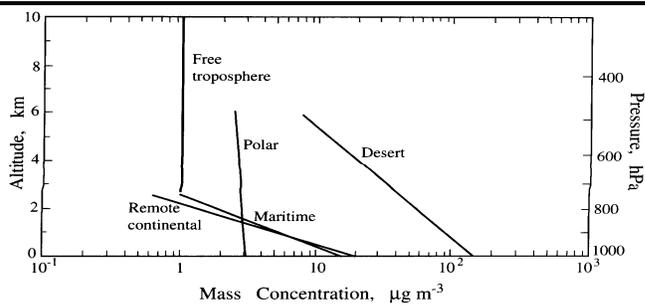


FIGURE 7.25 Representative vertical distribution of aerosol mass concentration (Jaenicke, 1993).

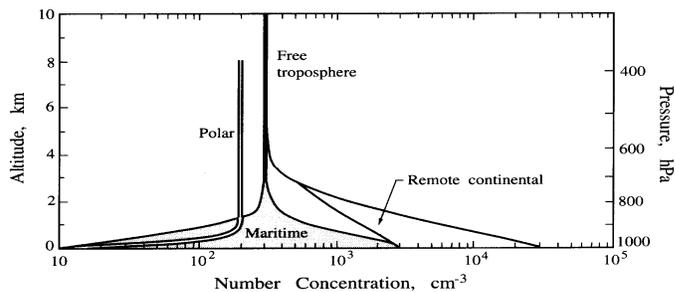


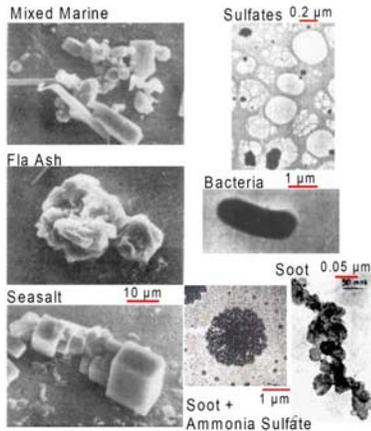
FIGURE 7.26 Representative vertical distribution of aerosol number concentration (Jaenicke, 1993). Seinfeld & Pandis

From Zhang

# Aerosol Sizes (Diameters)

From Zhang

- Aerosol sizes are usually reported as diameters.
- Yet many atmospheric particles have irregular shapes → have to use equivalent / effective diameter that depends on a physical property.



Details on PM diameters and shapes see:  
DeCarlo et al., *Particle morphology and density characterization by combined mobility and aerodynamic diameter measurements. Part 1: Theory, Aerosol Science & Technology*, 38, 1185-1205, 2004.

## Commonly used effective diameters:

**Aerodynamic diameter,  $d_a$ :** the diameter of a sphere of unit density ( $1 \text{ g cm}^{-3}$ ) that has the same terminal falling speed in air as the particle under consideration. Measured by inertial methods such as impactors and cyclones, depends on particle shape, density & size

**Electrical mobility diameter,  $d_m$ :** the diameter of a charged sphere with the same migration velocity of the charged particle under consideration in a constant electric field at atmospheric pressure. Obtained by electrostatic mobility analyzers (e.g., DMA) depends on particle shape and size.

**Vacuum aerodynamic diameter,  $d_{va}$ :** the diameter of a sphere, in the free molecular regime, with unit density ( $1 \text{ g/cm}^3$ ) and the same terminal velocity as the particle under consideration. Measured by e.g., Aerodyne AMS, under high vacuum, depends on particle shape, density & size.

**Optical diameter,  $d_o$ :** obtained by light scattering detectors, depends on particle refractive index, shape, and size.

# Effective Particle Diameters

Depending on the circumstance, different metrics are used for the particle size:

- ✓ **Classical aerodynamic diameter:** diameter of a sphere with density =  $1 \text{ g/cm}^3$  that has the same terminal velocity in a gravitational field as the particle under consideration
- ✓ **Stokes diameter:** same as above except that density of the reference spherical particle is the same as for the particle in question
- ✓ **Volume equivalent diameter:** diameter of a sphere with the same density that has the same volume as the non-spherical particle in question
- ✓ **Electrical mobility equivalent diameter:** diameter of a sphere with density =  $1 \text{ g/cm}^3$  that has the same mobility in electrostatic field as the particle under consideration.

Particle in an E-field:

$$qE = \frac{6\pi\eta\omega R_p}{C_c}$$

$$\omega = \left[ \frac{C_c}{6\pi\eta R_p} \right] \cdot qE$$

Stokes radius

Electric mobility

**Solve in class: Find volume equivalent diameter of a rod-like virus, which is  $1 \mu\text{m}$  long and  $0.1 \mu\text{m}$  wide. The effective density of the virus is  $1.1 \text{ g/cm}^3$**

**Solve in class: Find a relationship between aerodynamic and Stokes diameters**

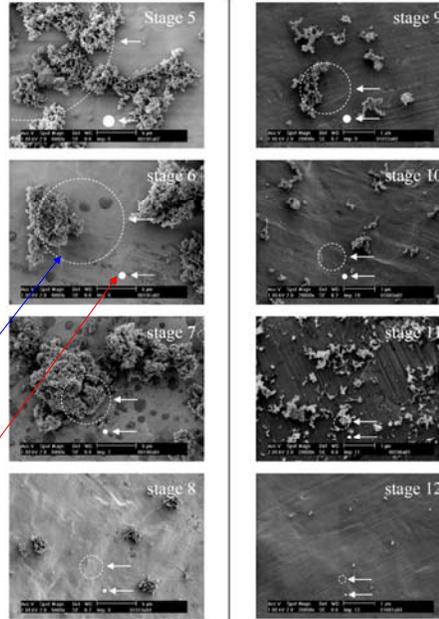
From Nidkorodov

# Aerosol Diameters

- Particle diameters are operationally defined
- Different measurement techniques may report enormously different numbers
- Be aware of the measurement technique!

Mobility diameter ( $D_m$ )

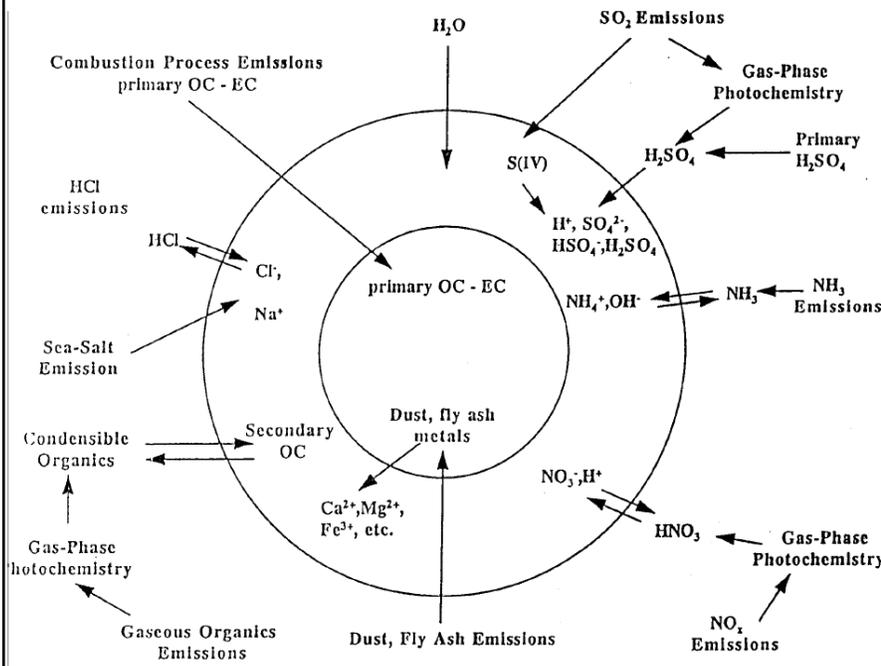
Aerodynamic diameter ( $D_a$ )



From Zhang

Fig. 5. Diesel soot on the ELPI-impactor stages 5–8 (5000 $\times$ ) and stages 9–12 (20,000 $\times$ ). White spots indicate aerodynamic upper size limit (previous impactor cutoff-size), white circles indicate corresponding mobility diameter (Table 3).

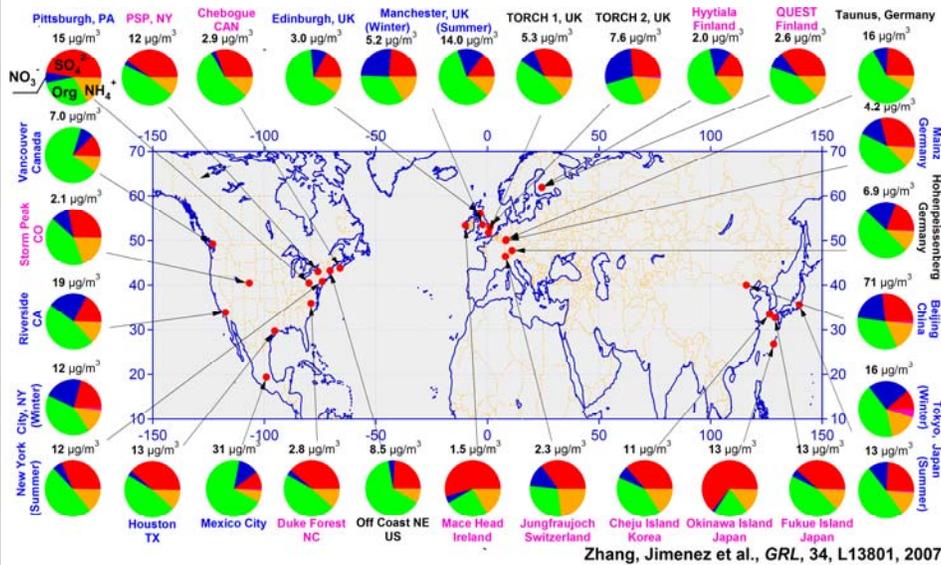
## Typical Chemical Composition of Atmospheric Aerosols



Adapted from Zhang

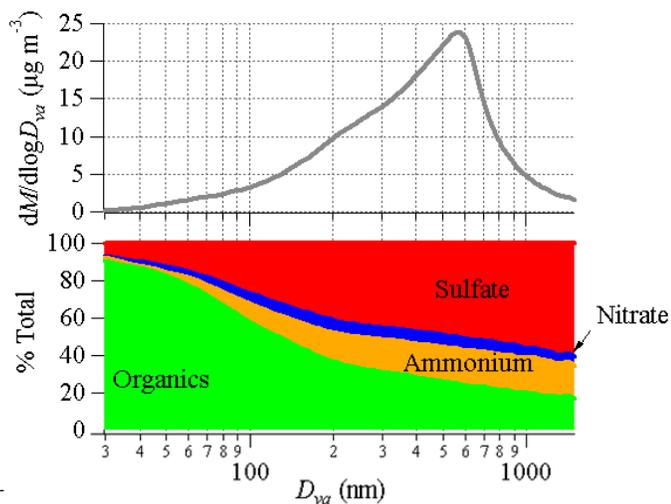
2003 NAI/RSSTO Assessment

## Submicron aerosol Composition in Northern Hemisphere



Does not include black carbon and other minor components (metals etc.)

## Size Resolved Composition of Pittsburgh Fine PM

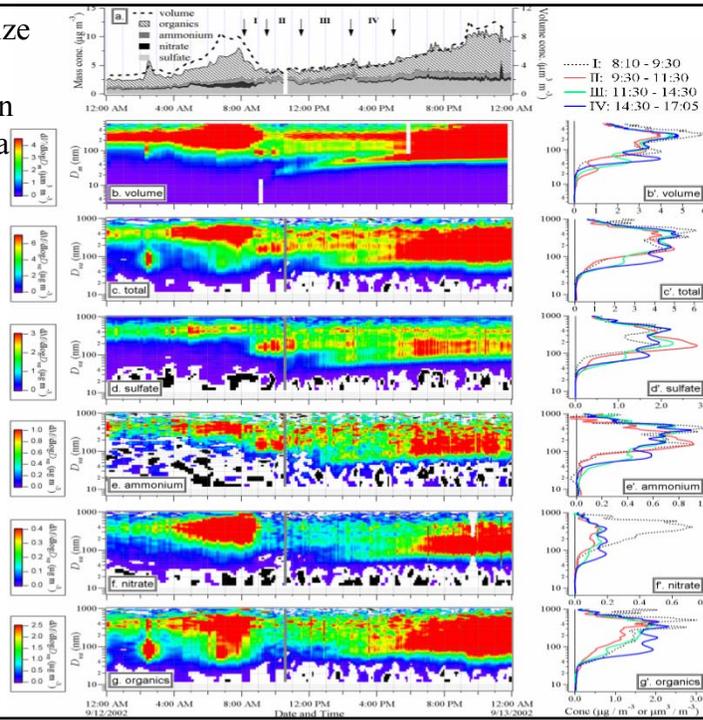


Zhang et al., Time and size-resolved chemical composition of submicron particles in Pittsburgh - Implications for aerosol sources and processes, *J. Geophys. Res.*, 110 (D07S09), 2005.

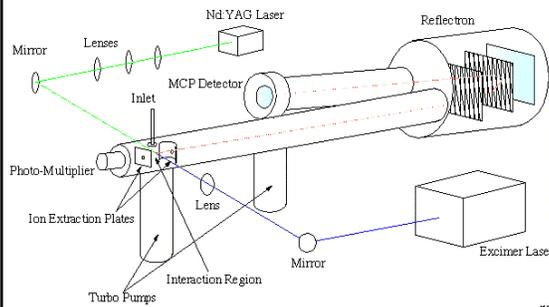
From Zhang

## Evolution of the size distributions of ambient aerosols in Pittsburgh during a nucleation day

Zhang et al., *Insights into the chemistry of new particle formation and growth events in Pittsburgh based on Aerosol Mass Spectrometry*, *Environmental Science & Technology*, 38 (18), 4797-4809, 2004.



## Single Particle Composition by Mass Spectrometry



PALMS designed by Dan Murphy at Aeronomy Lab  
<http://www.al.noaa.gov/PALMS/>.

Particle mass-spectrometers use lasers or heat to vaporize individual particles and analyze their compositions with either quadrupole or TOF MS. They provide valuable information about size distribution and composition of atmospheric aerosols. Jose-Luis Jimenez (CU Boulder) created an excellent compilation of existing aerosol mass spectrometers at <http://cires.colorado.edu/jimenez/ams.html>

From Nidkorodov

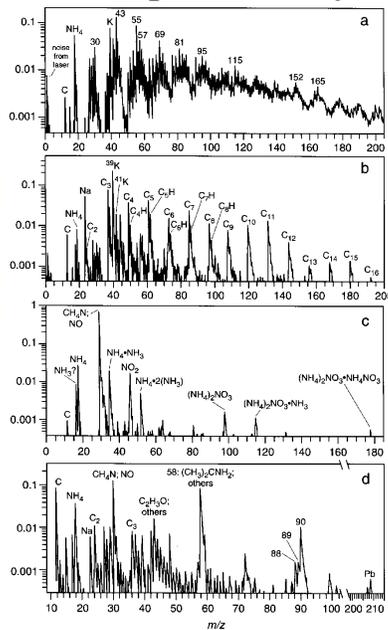


FIGURE 11.71 Typical laser ionization positive ion mass spectra of single particles in rural Colorado (adapted from Murphy and Thomson, 1997a,b).

# Atmospheric Aerosols III

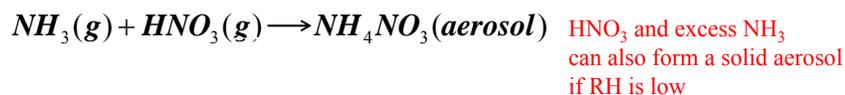
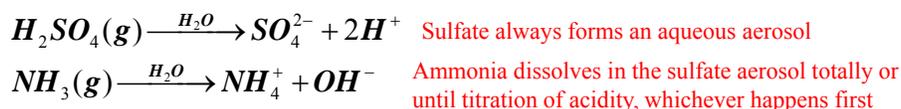
*Required reading: Jacob Chapter 8*

Atmospheric chemistry  
 ATOC-5151 / CHEM-5151  
 Spring 2013  
 Prof. J.L. Jimenez

Some slides adapted from lectures from Qi Zhang, Daniel Jacob, and Sergey Nidkorodov

## Formation of Ammonium / Nitrate / Sulfate Aerosols

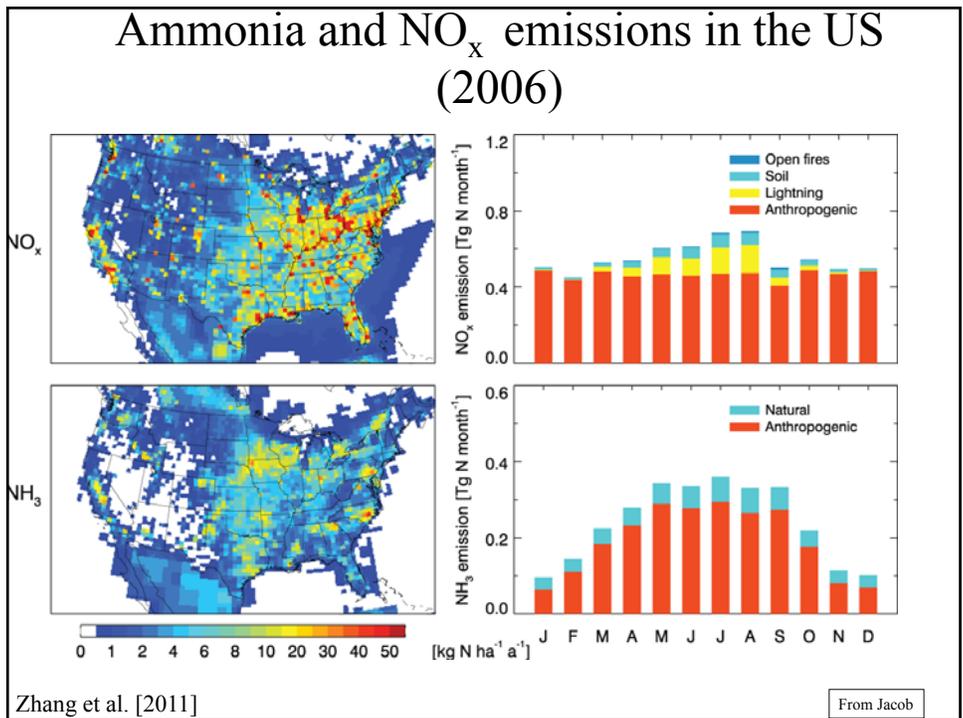
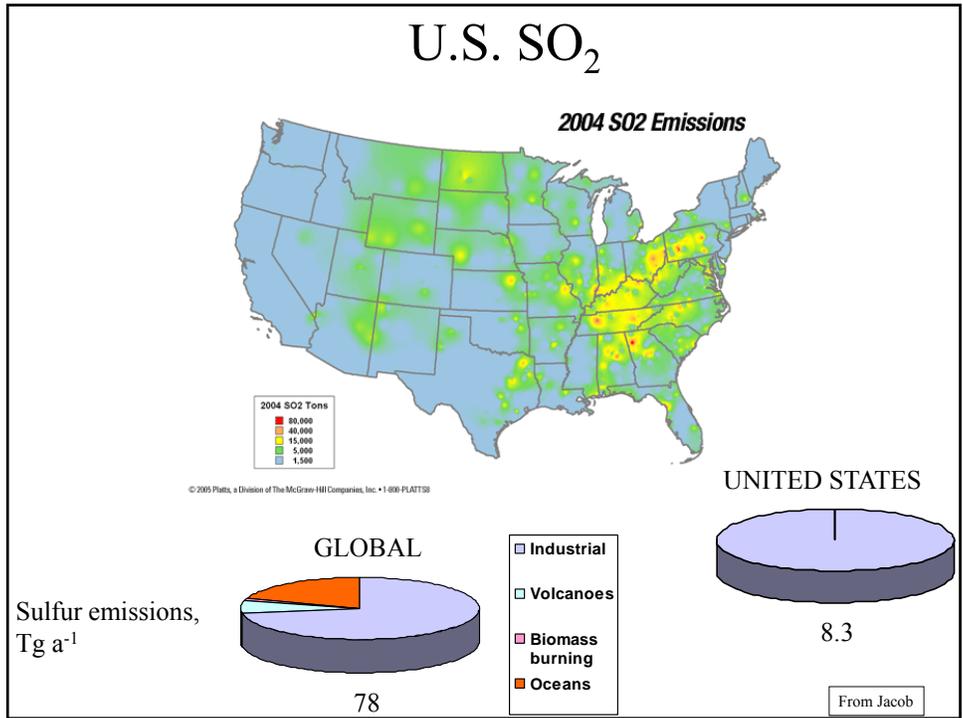
Thermodynamic rules:



| Condition                 | aerosol pH | Low RH   | High RH                                |
|---------------------------|------------|--|--|
| $[S(VI)] > 2[N(-III)]$    | acid       | $H_2SO_4 \cdot nH_2O$ ,<br>$NH_4HSO_4$ ,<br>$(NH_4)_2SO_4$ | $(NH_4^+, H^+, SO_4^{2-})$<br>solution |
| $[S(VI)] \leq 2[N(-III)]$ | neutral    | $(NH_4)_2SO_4$ ,<br>$NH_4NO_3$                             | $(NH_4^+, NO_3^-)$<br>solution         |

E.g. AIM model: <http://www.aim.env.uea.ac.uk/aim/aim.php>

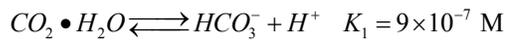
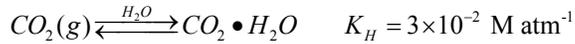
From Jacob



# Natural pH of Rain

- $\text{H}_2\text{O}(\text{l}) \leftrightarrow \text{H}^+(\text{aq}) + \text{OH}^-(\text{aq})$        $K_w = [\text{H}^+][\text{OH}^-] = 1.01 \times 10^{-14}$  at 25 °C
- In pure water  $[\text{H}^+] = [\text{OH}^-]$        $K_w = [\text{H}^+][\text{OH}^-] = (x)(x) = 1.01 \times 10^{-14}$
- $\text{pH} = -\log_{10}([\text{H}^+]) = 7$        $x = [\text{H}^+] = [\text{OH}^-] = 1.01 \times 10^{-7} \text{ M}$
- for further reference see e.g. [http://preparatorychemistry.com/Bishop\\_pH\\_Equilibrium.htm](http://preparatorychemistry.com/Bishop_pH_Equilibrium.htm)

- Equilibrium with natural  $\text{CO}_2$  (280 ppmv) results in a rain pH of 5.7:

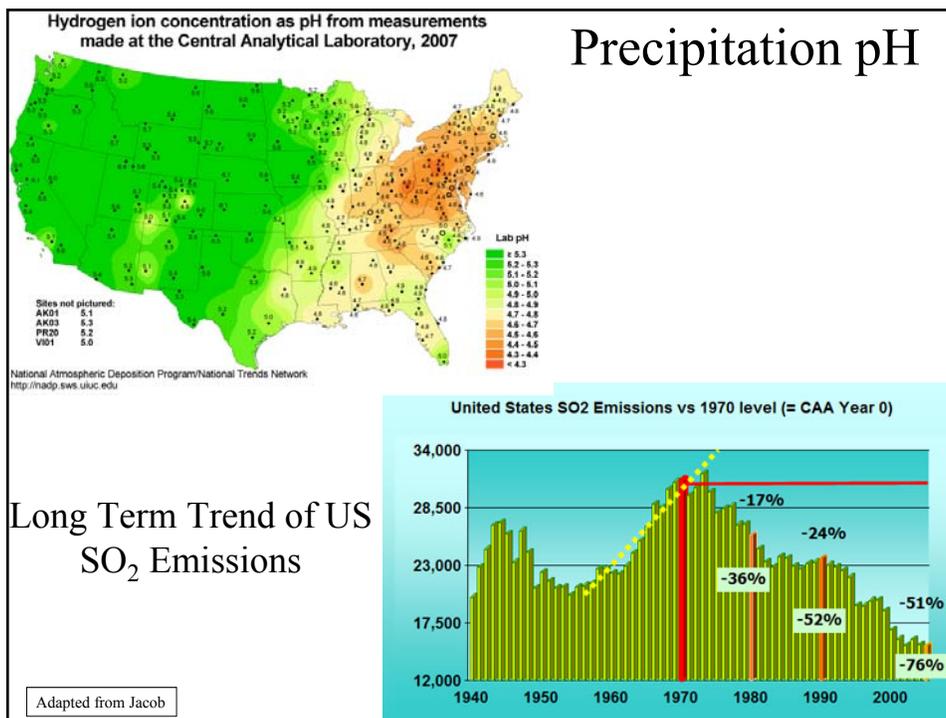


$$\Rightarrow [\text{H}^+] = (K_1 K_H P_{\text{CO}_2})^{1/2}$$

- This pH can be modified by natural acids ( $\text{H}_2\text{SO}_4$ ,  $\text{HNO}_3$ ,  $\text{RCOOH}$ ...) and bases ( $\text{NH}_3$ ,  $\text{CaCO}_3$ )  $\Rightarrow$  natural rain has a pH in range 5-7

“Acid rain” refers to rain with  $\text{pH} < 5 \Rightarrow$  damage to ecosystems

From Jacob



But ecosystem acidification is partly a titration problem from acid input over many years

Acid flux  
 $F_{H^+}$

Acid-neutralizing capacity (ANC)  
 from  $CaCO_3$  and other bases

$$\int_0^t F_{H^+} dt > ANC \Rightarrow \text{acidification}$$

From Jacob

## Elemental & Organic Carbon (EC/OC)

EC: elemental carbon

OC: organic carbon

Soot: a by product of the combustion, contain both EC and OC. Present as chain agglomerate of small roughly spherical elementary carbonaceous particles.  
 $\rho \approx 1.8 \text{ g/cm}^3$

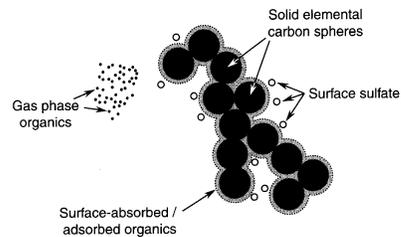
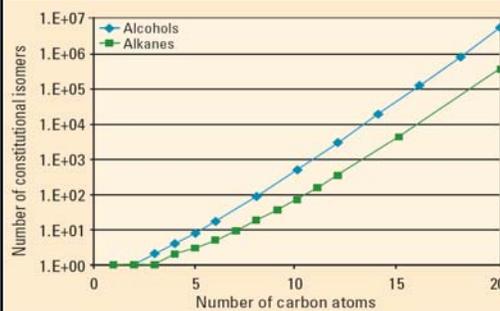


FIGURE 10.1 Schematic of a diesel soot particle consisting of an agglomeration of elemental carbon spheres (0.01- to 0.08- $\mu\text{m}$  diameter). Its surface is covered with absorbed/adsorbed particle-phase organics, including 5-ring (e.g., BaP) and 6-ring PAHs. Gas-phase organics include all of the highly volatile 2-ring PAHs (e.g., naphthalene and methylnaphthalenes). Semivolatile 3-ring (e.g., phenanthrene and anthracene) and 4-ring PAHs (e.g., pyrene (II) and fluoranthene (V)) are distributed between both phases. Sulfate is also associated with diesel particles. (Adapted with permission from Johnson *et al.*, 1994, SAE Paper 940233 © 940233 Society of Automotive Engineers, Inc.; see also Schauer *et al.*, 1999.)

Finlayson-Pitts & Pitts

OC: thousands of compounds, extremely complex

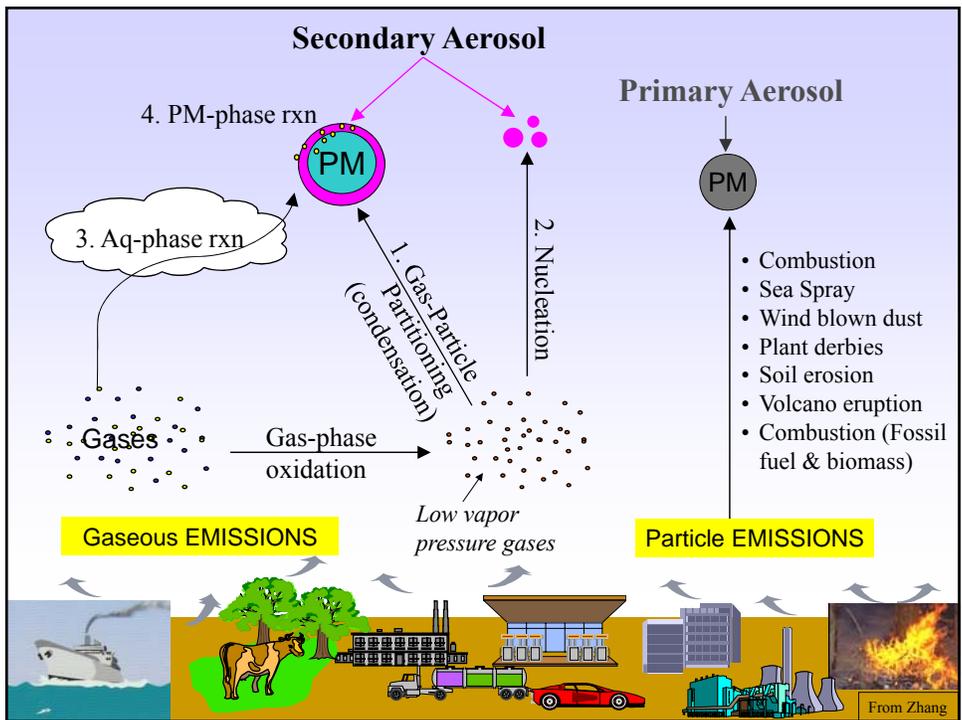
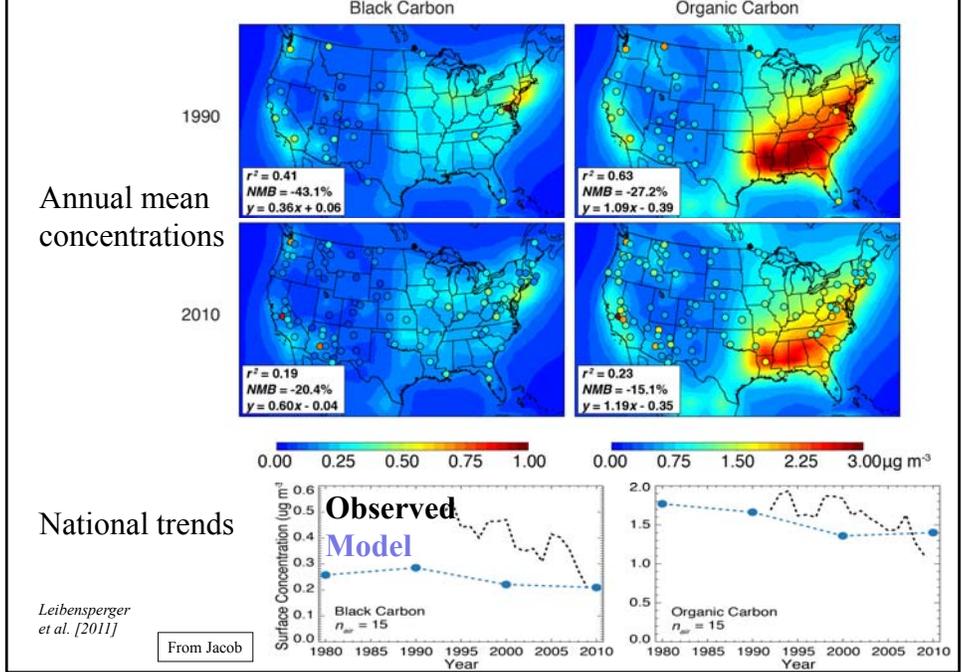
Number of unique isomers for alkanes and alcohols

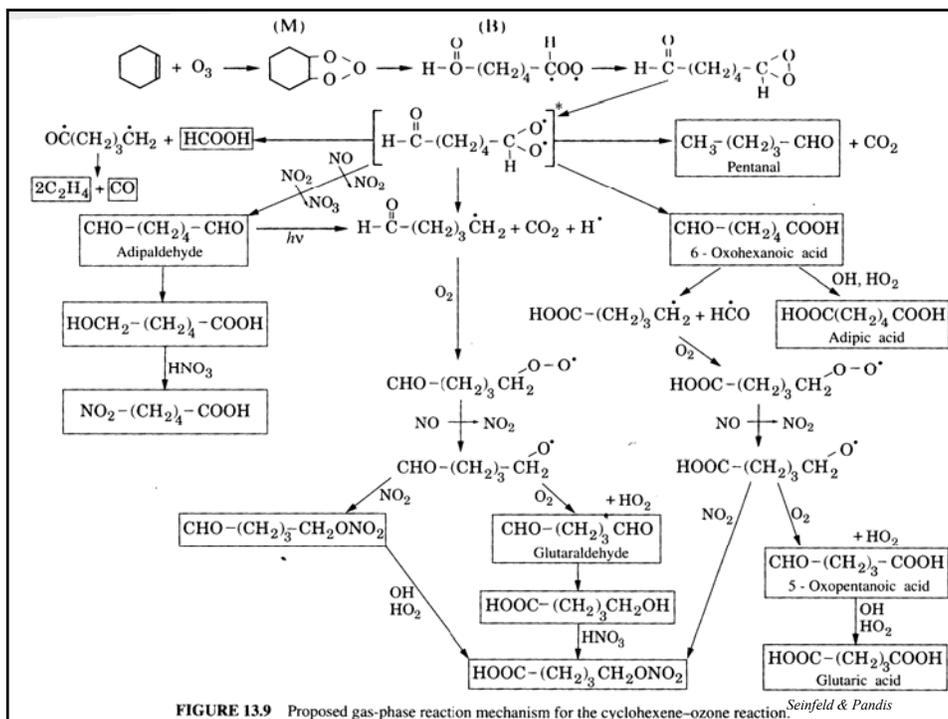


← Goldstein & Galbally, ES&T 2007

Adapted from Zhang

# Long-term trends in BC and OC aerosol over the US





## Organic Aerosol Analysis

- Organic aerosols are composed of thousands of compounds.
- Chemical analysis is a significant challenge.
- Compound specific study can only explain a small fraction of total organic mass. Large fraction unidentified.
- A number of analytical methods are available, they are complementary.

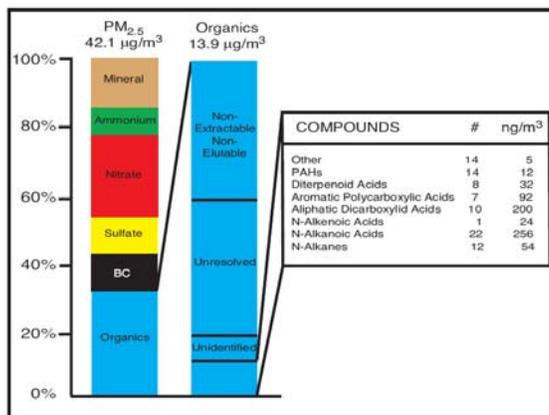
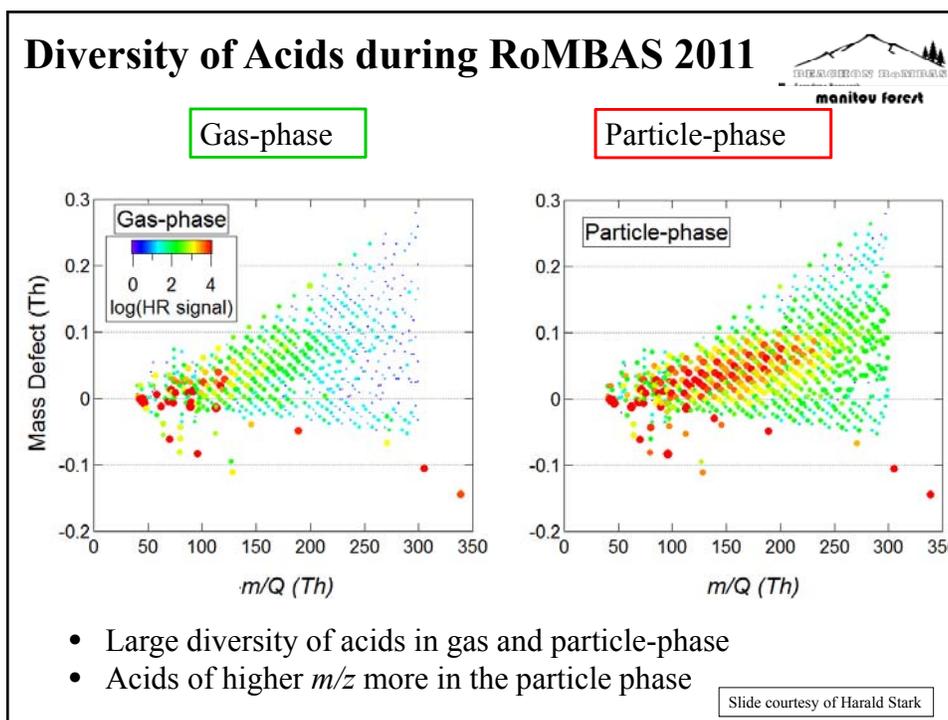
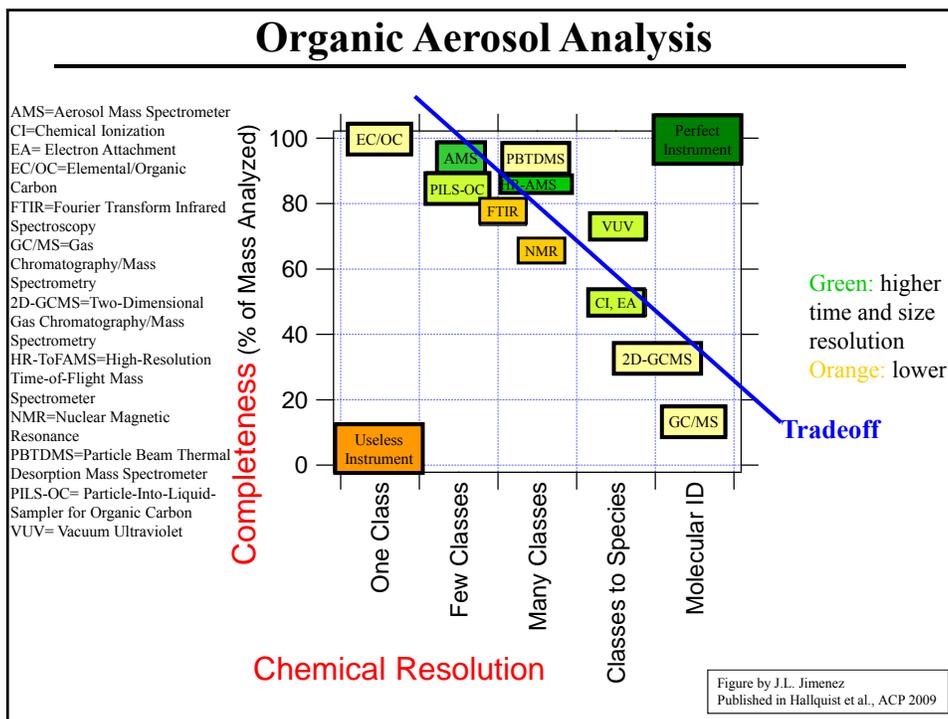
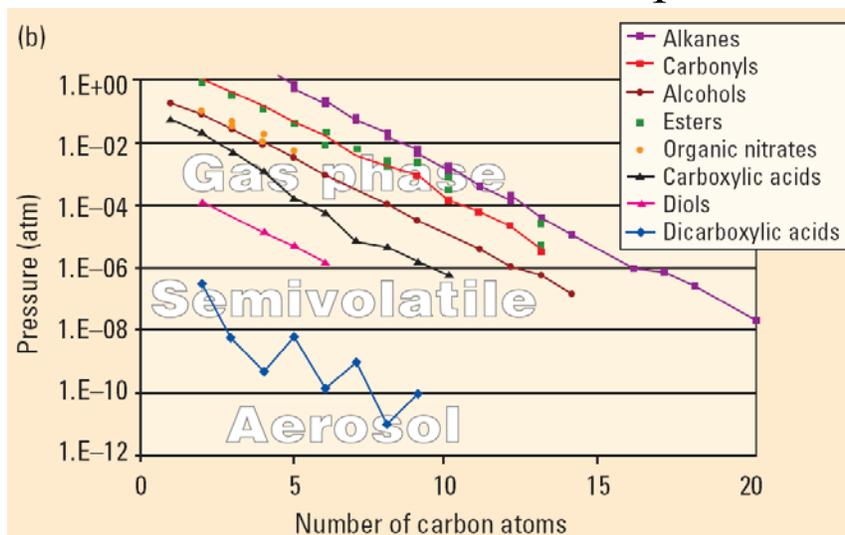


Figure 3.10. Speciation results for organic aerosol in Southern California (Rogge et al., 1993). Even if a hundred or so individual organic compounds were identified and quantified they represented only 15 percent or so of the total organic mass. *2003 NARSTO Assessment*

From Zhang



## Gas-Phase vs Aerosol Compounds



- For monofunctional compounds, alkanes beyond C<sub>20</sub> and acids beyond C<sub>3</sub> will partition to aerosols

Goldstein & Galbally,  
ES&T 2007

## Gas/particle partitioning Theory

**Data:** Fraction in particle-phase,  $F_p$

$$F_p = \frac{\text{Particle}}{\text{Gas} + \text{Particle}}$$

**Model:** Absorptive partitioning theory using effective saturation concentration ( $C_i^*$ )

$$F_{p,i} = \left(1 + \frac{C_i^*}{C_{OA}}\right)^{-1}$$

$$C_i^* = \frac{M_i 10^6 \zeta_i P_{L,i}^o}{760 RT}$$

**Model Inputs:**  $T$  (K) = Ambient temperature

$C_{OA}$  ( $\mu\text{g m}^{-3}$ ) = Organic aerosol mass concentration

$P_{L,i}^o$  (torr) = Vapor pressures of compound  $i$  (at  $T$ )

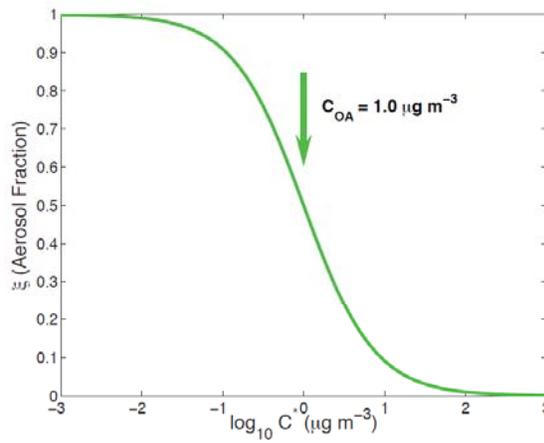
$\zeta_i$  = Activity coefficient of compound  $i = 1$

$M_i$  ( $\text{g mol}^{-1}$ ) = Molecular weight of compound  $i$

(Pankow, AE 1994; Donahue et al., ES&T 2006)

## Partitioning of an individual species vs $c^*$

$$\xi_i = \frac{1}{1 + \frac{C_i^*}{C_{OA}}}$$

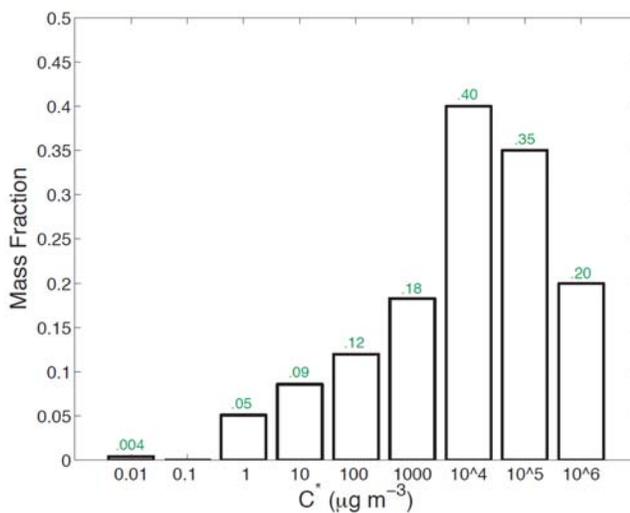


The bottom line is that an individual component only 'cares' about the *total* mass of the solution compared to its saturation concentration. For example, a  $1 \mu\text{g m}^{-3} C^*$  component will be 50-50 partitioned if there is  $1 \mu\text{g m}^{-3}$  total organic aerosol, no matter what its composition.

Donahue et al., ES&T 2006. Slide courtesy of Neil Donahue

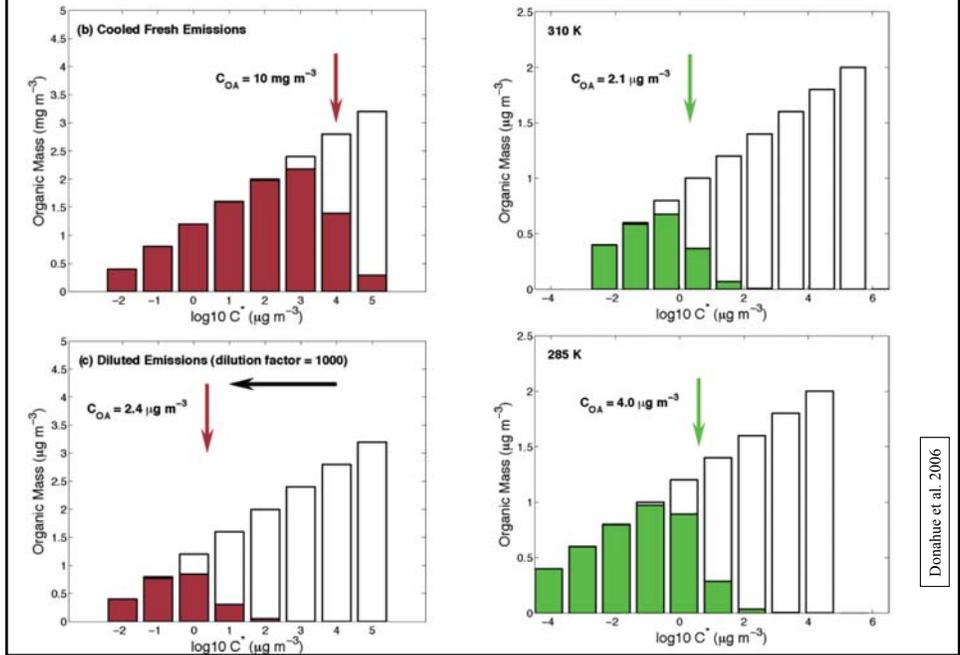
## Basis Set 101: Calculate % Partitioning of $\alpha$ -pinene SOA when $C_{OA} = 10 \mu\text{g m}^{-3}$

- $\alpha\text{-pinene} + \text{O}_3 \rightarrow 0.004 P_{0.01} + 0.1 P_{0.1} + \dots$



Adapted from Neil Donahue

# Cooling & Dilution in VBS



# Aging in the Volatility Basis Set

